Note

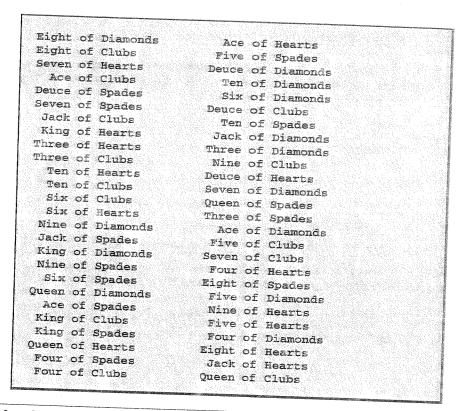


Fig. 16.3 Output for the high-performance card shuffling and dealing simulation.

16.7 Bitwise Operators

C++ provides extensive bit manipulation capabilities for programmers who need to get down to the so-called "bits-and-bytes" level. Operating systems, test equipment software, networking software, and many other kinds of software require that the programmer communicate "directly with the hardware." In this and the next several sections, we discuss C++'s bit manipulation capabilities. We introduce each of C++'s many bitwise operators and we discuss how to save memory by using bit fields.

All data is represented internally by computers as sequences of bits. Each bit can assume the value **0** or the value **1**. On most systems, a sequence of 8 bits forms a byte—the standard storage unit for a variable of type **char**. Other data types are stored in larger numbers of bytes. The bitwise operators are used to manipulate the bits of integral operands (**char**, **short**, **int**, and **long**; both **signed** and **unsigned**). Unsigned integers are normally used with the bitwise operators.



Portability Tip 16.3

Bitwise data manipulations are machine dependent.

tions of the number s and 16.8 byte) int program The OR(A), 8€, <<, 8 bitwise operanc respond result to OR op is 1. Tl specifi right b sets al

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) simulation.

need to get ent software, ammer com-, we discuss se operators

Each bit can ms a byte red in larger ral operands integers are Note that the bitwise operator discussions in this section show the binary representations of the integer operands. For a detailed explanation of the binary (also called base 2) number system see the appendix, "Number Systems". Also, the programs in Sections 16.7 and 16.8 were tested on a PC compatible using Borland C++. This system uses 16-bit (2-byte) integers. Because of the machine-dependent nature of bitwise manipulations, these programs may not work on your system.

The bitwise operators are: bitwise AND (&), bitwise inclusive OR(||), bitwise exclusive $OR(||^*)$, left shift (<<), right shift (>>), and complement (~). (Note that we have been using &, <<, and >> for other purposes. This is a classic example of operator overloading.) The bitwise AND, bitwise inclusive OR, and bitwise exclusive OR operators compare their two operands bit-by-bit. The bitwise AND operator sets each bit in the result to 1 if the corresponding bit in both operands is 1. The bitwise inclusive OR operator sets each bit in the result to 1 if the corresponding bit in either (or both) operand(s) is 1. The bitwise exclusive OR operator sets each bit in the result to 1 if the corresponding bit in exactly one operand is 1. The left shift operator shifts the bits of its left operand to the left by the number of bits specified in its right operand. The right shift operand to the left by the number of bits specified in its right operand. The bitwise complement operator sets all 0 bits in its operand to 1 in the result and sets all 1 bits to 0 in the result. Detailed discussions of each bitwise operator appear in the following examples. The bitwise operators are summarized in Fig. 16.4.

When using the bitwise operators, it is useful to print values in their binary representation to illustrate the precise effects of these operators. The program of Fig. 16.5 prints an unsigned integer in its binary representation in groups of eight bits each. Function displayBits uses the bitwise AND operator to combine variable value with variable displayMask. Often, the bitwise AND operator is used with an operand called a mask—an integer value with specific bits set to 1. Masks are used to hide some bits in a value while selecting other bits. In displayBits, mask variable displayMask is assigned the value 1 << 15 (10000000 0000000). The left shift operator shifts the value 1 from the low order (rightmost) bit to the high order (leftmost) bit in displayMask, and fills in 0 bits from the right. The statement

Operator	Name	Description
&:	bitwise AND	The bits in the result are set to 1 if the corresponding bits in the two operands are both 1.
	bitwise inclusive OR	The bits in the result are set to 1 if at least one of the corresponding bits in the two operands is 1.
^	bitwise exclusive OR	The bits in the result are set to 1 if exactly one of the corresponding bits in the two operands is 1.
<<	left shift	Shifts the bits of the first operand left by the number of bits specified by the second operand; fill from right with 0 bits.

Fig. 16.4 The bitwise operators (part 1 of 2).

Fig. 16.4 The bitwise operators (part 2 of 2).

```
// Fig. 16.5: fig16_05.cpp
      // Printing an unsigned integer in bits
      #include <iostream.h>
      #include <iomanip.h>
  5
     void displayBits( unsigned );
  6
  8
     int main()
  9
 10
         unsigned x;
 11
 12
        cout << "Enter an unsigned integer: ";
 13
         cin >> x;
 14
        displayBits( x );
 15
        return 0;
 16
 17
    void displayBits( unsigned value )
 18
19
20
        unsigned c, displayMask = 1 << 15;
21
22
        cout << setw( 7 ) << value << " = ";
23
24
        for ( c = 1; c <= 16; c++ ) {
25
           cout << ( value & displayMask ? '1' : '0' );</pre>
26
           value <<= 1;</pre>
27
28
           if ( c % 8 == 0 )
29
              cout << ' ';
30
        }
31
32
       cout << endl;
33
```

Enter an unsigned integer: 65000 65000 = 11111101 11101000

Fig. 16.5 Printing an unsigned integer in bits.



number of bits of filling from

n

```
cout << ( value & displayMask ? '1' : '0' );</pre>
```

determines whether a 1 or a 0 should be printed for the current leftmost bit of variable value. Assume variable value contains 65000 (11111101 11101000). When value and displayMask are combined using &, all the bits except the high order bit in variable value are "masked off" (hidden) because any bit "ANDed" with 0 yields 0. If the leftmost bit is 1, value & displayMask evaluates to 10000000 00000000 (which is interpreted as true, and 1 is printed—otherwise, 0 is printed. Variable value is then left shifted one bit by the expression value <<= 1 (this is equivalent to the assignment value = value << 1). These steps are repeated for each bit variable value. Figure 16.6 summarizes the results of combining two bits with the bitwise AND operator.

Common Programming Error 16.5



Using the logical AND operator (&&) for the bitwise AND operator (&) and vice versa.

The program of Fig. 16.7 demonstrates the use of the bitwise AND operator, the bitwise inclusive OR operator, the bitwise exclusive OR operator, and the bitwise complement operator. The program uses function **displayBits** to print the **unsigned** integer values. The output is shown in Fig. 16.8.

Bit 1 Bit 2 Bit 1 & Bit	it2
0 0	
1 0 0	
0 1 0	
1 1	

Fig. 16.6 Results of combining two bits with the bitwise AND operator (&).

```
// Fig. 16.7: fig16_07.cpp
    // Using the bitwise AND, bitwise inclusive OR, bitwise
    // exclusive OR, and bitwise complement operators.
 4
    #include <iostream.h>
 5
    #include <iomanip.h>
   void displayBits( unsigned );
 8
9
    int main()
10
11
       unsigned number1, number2, mask, setBits;
12
13
       number1 = 65535;
14
       mask = 1;
```

Fig. 16.7 Using the bitwise AND, bitwise inclusive OR, bitwise exclusive OR, and bitwise complement operators (part 1 of 2).



```
15
           cout << "The result of combining the following \n";
    16
           displayBits( number1 );
    17
           displayBits( mask );
    18
           cout << "using the bitwise AND operator & is\n";</pre>
    19
           displayBits( number1 & mask );
   20
   21
           number1 = 15;
   22
           setBits = 241;
   23
           cout << "\nThe result of combining the following\n";
   24
          displayBits( number1 );
   25
          displayBits( setBits );
   26
          cout << "using the bitwise inclusive OR operator | is\n";
   27
          displayBits( number1 | setBits );
   28
  29
          number1 = 139;
  30
          number2 = 199;
  31
          cout << "\nThe result of combining the following\n";</pre>
  32
          displayBits( number1 );
  33
         displayBits( number2 );
  34
         cout << "using the bitwise exclusive OR operator ^ is\n";</pre>
  35
         displayBits( number1 ^ number2 );
  36
  37
         number1 = 21845;
  38
         cout << "\nThe one's complement of\n";</pre>
  39
         displayBits( number1 );
 40
         cout << "is" << endl;
 41
         displayBits( ~number1 );
 42
 43
         return 0;
 44
 45
     void displayBits( unsigned value )
 46
 47
 48
        unsigned c, displayMask = 1 << 15;
 49
 50
        cout << setw( 7 ) << value << " = ";
 51
52
        for ( c = 1; c <= 16; c++ ) {
53
           cout << ( value & displayMask ? '1' : '0' );</pre>
54
           value <<= 1;
55
56
           if (c % 8 == 0)
57
              cout << ' ';
58
59
60
       cout << endl;
61
    }
```

Fig. 16.7 Using the bitwise AND, bitwise inclusive OR, bitwise exclusive OR, and bitwise complement operators (part 2 of 2).

1 18 0

is\n";

is\n";

OR, and

```
The result of combining the following
  65535 = 11111111 11111111
      1 = 00000000 00000001
using the bitwise AND operator & is
      1 = 00000000 00000001
The result of combining the following
    15 = 00000000 00001111
    241 = 00000000 11110001
using the bitwise inclusive OR operator | is
    255 = 00000000 11111111
The result of combining the following
    139 = 00000000 10001011
    199 = 00000000 11000111
using the bitwise exclusive OR operator * is
     76 = 00000000 01001100
The one's complement of
  21845 = 01010101 01010101
  43690 = 10101010 10101010
```

Fig. 16.8 Output for the program of Fig. 16.7.

In Fig. 16.7, variable mask is assigned the value 1 (0000000 0000001), and variable number1 is assigned value 65535 (11111111 1111111). When mask and number1 are combined using the bitwise AND operator (&) in the expression number1 & mask, the result is 00000000 0000001. All the bits except the low order bit in variable number1 are "masked off" (hidden) by "ANDing" with variable mask.

The bitwise inclusive OR operator is used to set specific bits to 1 in an operand. In Fig. 16.7, variable number1 is assigned 15 (0000000 00001111), and variable setBits is assigned 241 (0000000 11110001). When number1 and setBits are combined using the bitwise OR operator in the expression number1 | setBits, the result is 255 (0000000 111111111). Figure 16.9 summarizes the results of combining two bits with the bitwise inclusive OR operator.



Common Programming Error 16.6

Using the logical OR operator (| | |) for the bitwise OR operator (| |) and vice versa.

The bitwise exclusive OR operator (^) sets each bit in the result to 1 if exactly one of the corresponding bits in its two operands is 1. In Fig. 16.7, variables number1 and number2 are assigned the values 139 (0000000 10001011) and 199 (0000000 11000111). When these variables are combined with the exclusive OR operator in the expression number1 ^ number2, the result is 00000000 01001100. Figure 16.10 summarizes the results of combining two bits with the bitwise exclusive OR operator.

Bif 1	Bit 2	Bit 1 Bit 2
0	0	Q
1	. 0	1
0	1	1.
1	1	1
	•	

Fig. 16.9 Results of combining two bits with the bitwise inclusive OR operator (1).

Bif 1	Bit 2	Bit 1 * Bit 2
0	0	
1	0	U
0	1.	.E. 19
1	1	0
		ŭ

Fig. 16.10 Results of combining two bits with the bitwise exclusive OR operator (*).

The bitwise complement operator (~) sets all 1 bits in its operand to 0 in the result and sets all 0 bits to 1 in the result—otherwise referred to as "taking the one's complement of the value." In Fig. 16.7, variable number1 is assigned the value 21845 (01010101 01010101). When the expression ~number1 is evaluated, the result is (10101010 10101010).

The program of Fig. 16.11 demonstrates the left shift operator (<<) and the right shift operator (>>). Function **displayBits** is used to print the **unsigned** integer values.

```
// Fig. 16.11: fig16_11.cpp
    // Using the bitwise shift operators
    #include <iostream.h>
    #include <iomanip.h>
    void displayBits( unsigned );
 8
    int main()
10
       unsigned number1 = 960;
17
12
       cout << "The result of left shifting \n^n;
13
       displayBits( number1 );
14
       cout << "8 bit positions using the left "
15
            << "shift operator is\n";
```

Fig. 16.11 Using the bitwise shift operators (part 1 of 2).

∍rator (∣).

erator (*).

result and plement of

1010101

0101010

right shift

r values.

```
displayBits( number1 << 8 );
17
       cout << "\nThe result of right shifting\n";</pre>
18
       displayBits( number1 );
19
       cout << "8 bit positions using the right "
20
             << "shift operator is\n";
21
       displayBits( number1 >> 8 );
22
       return 0;
23
24
25
    void displayBits (unsigned value)
26
27
       unsigned c, displayMask = 1 << 15;
28
29
       cout << setw( 7 ) << value << " = ";</pre>
30
31
       for (c = 1; c <= 16; c++) {
32
           cout << ( value & displayMask ? '1' : '0' );</pre>
33
           value <<= 1;
34
35
           if ( c % 8 == 0 )
36
              cout << ' ';
37
        }
38
39
        cout << endl;
40
    }
```

```
The result of left shifting
   960 = 00000011 11000000

8 bit positions using the left shift operator << is
   49152 = 11000000 00000000

The result of right shifting
   960 = 00000011 11000000

8 bit positions using the right shift operator >> is
   3 = 00000000 00000011
```

Fig. 16.11 Using the bitwise shift operators (part 2 of 2).

The left shift operator (<<) shifts the bits of its left operand to the left by the number of bits specified in its right operand. Bits vacated to the right are replaced with 0s; 1s shifted off the left are lost. In the program of Fig. 16.11, variable number1 is assigned the value 960 (0000011 11000000). The result of left shifting variable number1 8 bits in the expression number1 << 8 is 49152 (11000000 00000000).

The right shift operator (>>) shifts the bits of its left operand to the right by the number of bits specified in its right operand. Performing a right shift on an **unsigned** integer causes the vacated bits at the left to be replaced by 0s; 1s shifted off the right are lost. In the program of Fig. 16.11, the result of right shifting **number1** in the expression **number1** >> 8 is 3 (00000000 0000011).



Common Programming Error 16.7

The result of shifting a value is undefined if the right operand is negative or if the right operand is larger than the number of bits in which the left operand is stored.



Portability Tip 16.4

The result of right shifting a signed value is machine dependent. Some machines fill with zero and others use the sign bit.

Each bitwise operator (except the bitwise complement operator) has a corresponding assignment operator. These *bitwise assignment operators* are shown in Fig. 16.12 and are used in a similar manner to the arithmetic assignment operators introduced in Chapter 2.

Figure 16.13 shows the precedence and associativity of the various operators introduced to this point in the text. They are shown top to bottom in decreasing order of precedence.

&= Bitwise AND assignment operator.	
Bitwise inclusive OR assignment operator.	
A Bitwise exclusive OR assignment operator.	
<== Left shift assignment operator.	
>>= Right shift with sign extension assignment operator.	

Fig. 16.12 The bitwise assignment operators.

Оре	∍rators						Associativity	Туре
	unary;	right (to left)	:	: (binary; left	to right)	left to right	highest
()	[]	•	->				left to right	highest
*	Б с	+ new	7	!	delete	sizeof	right to left	unary
*		%	· · · · · · · · · · · · · · · · · · ·				left to right	multiplicative
+	pas .	·					left to right	additive
<< <	>>						left to right	shifting
	<=	>	>=				left to right	relational
= == }							left to right	equality
ж 							left to right	bitwise AND
							left to right	bitwise XOR
							left to right	bitwise OR

Fig. 16.13 Operator precedence and associativity (part 1 of 2).

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St. &c	left to right	I - ' - I ANTIN
		logical AND
	left to right	logical OR
?:	right to left	conditional
- += -= *= /= %= %= = ^= <<= >>=	right to left	assignment

Fig. 16.13 Operator precedence and associativity (part 2 of 2).

16.8 Bit Fields

C++ provides the ability to specify the number of bits in which an **unsigned** or **int** member of a class or a structure (or a union—see Chapter 18, "Other Topics") is stored. Such a member is referred to as a *bit field*. Bit fields enable better memory utilization by storing data in the minimum number of bits required. Bit field members *must* be declared as **int** or **unsigned**.



Performance Tip 16.2

Bit fields help conserve storage.

Consider the following structure definition:

```
struct BitCard {
  unsigned face : 4;
  unsigned suit : 2;
  unsigned color : 1;
};
```

The definition contains three **unsigned** bit fields—**face**, **suit**, and **color**—used to represent a card from a deck of 52 cards. A bit field is declared by following an **unsigned** or **int** member with a colon (:) and an integer constant representing the *width* of the field (i.e., the number of bits in which the member is stored). The width must be an integer constant between 0 and the total number of bits used to store an **int** on your system. Our examples were tested on a computer with 2-byte (16 bit) integers.

The preceding structure definition indicates that member **face** is stored in 4 bits, member **suit** is stored in 2 bits, and member **color** is stored in 1 bit. The number of bits is based on the desired range of values for each structure member. Member **face** stores values between **0** (Ace) and **12** (King)—4 bits can store a value between 0 and 15. Member suit stores values between **0** and **3** (**0** = Diamonds, **1** = Hearts, **2** = Clubs, **3** = Spades)—2 bits can store a value between **0** and **3**. Finally, member **color** stores either **0** (Red) or **1** (Black)—1 bit can store either **0** or **1**.

The program in Fig. 16.14 (output shown in Fig. 16.15) creates array **deck** containing 52 **struct bitCard** structures. Function **fillDeck** inserts the 52 cards in the **deck** array, and function **deal** prints the 52 cards. Notice that bit field members of structures

are accessed exactly as any other structure member. The member **color** is included as a means of indicating the card color on a system that allows color displays.

```
// Fig. 16.14: fig16_14.cpp
       // Example using a bit field
    3
       #include <iostream.h>
       #include <iomanip.h>
       struct BitCard {
          unsigned face : 4;
   8
          unsigned suit : 2;
   9
          unsigned color : 1;
  10
      };
  11
  12
      void fillDeck( BitCard * );
  13
      void deal( BitCard * );
  14
  15
      int main()
  16
      {
  17
         BitCard deck[ 52 ];
  18
  19
         fillDeck( deck );
  20
         deal( deck );
 21
         return 0;
 22
 23
     void fillDeck( BitCard *wDeck )
 24
 25
 26
        for ( int i = 0; i <= 51; i++ ) {
 27
           wDeck[ i ].face = i % 13;
 28
           wDeck[ i ].suit = i / 13;
 29
           wDeck[ i ].color = i / 26;
 30
 31
     }
 32
    // Output cards in two column format. Cards 0-25 subscripted
    // with k1 (column 1). Cards 26-51 subscripted k2 in (column 2.)
    void deal( BitCard *wDeck )
35
36
37
       for ( int k1 = 0, k2 = k1 + 26; k1 \le 25; k1++, k2++ ) {
38
          cout << "Card:" << setw( 3 ) << wDeck[ k1 ].face</pre>
39
                << " Suit: " << setw( 2 ) << wDeck[ k1 ].suit
40
               << " Color:" << setw( 2 ) << wDeck[ k1 ].color
47
                      " << "Card:" << setw( 3 ) << wDeck[ k2 ].face
42
               << " Suit:" << setw( 2 ) << wDeck[ k2 ].suit
43
               << " Color: " << setw( 2 ) << wDeck[ k2 ].color
44
               << endl;
45
46
    }
```

Fig. 16.14 Using bit fields to store a deck of cards.

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n 2.)

.face

```
Suit: 0 Color: 0 Card: 0 Suit: 2 Color: 1
     0
Card:
                         Card: 1 Suit: 2 Color: 1
Card: 1
        Suit: 0 Color: 0
        Suit: 0 Color: 0 Card: 2 Suit: 2 Color: 1
                         Card: 3
                                   Suit: 2 Color: 1
        Suit: 0 Color: 0
Card: 3
        Suit: 0 Color: 0
                          Card: 4
                                   Suit: 2 Color: 1
Card: 4
                          Card: 5 Suit: 2 Color: 1
        Suit: 0 Color: 0
Card: 5
                         Card: 6 Suit: 2 Color: 1
Card: 6
Card: 7
     6
        Suit: 0 Color: 0
        Suit: 0 Color: 0 Card: 7 Suit: 2 Color: 1
Card: 8
        Suit: 0 Color: 0 Card: 8 Suit: 2 Color: 1
Card: 9 Suit: 0 Color: 0 Card: 9 Suit: 2 Color: 1
Card: 10 Suit: 0 Color: 0 Card: 10 Suit: 2 Color: 1
Card: 11 Suit: 0 Color: 0 Card: 11 Suit: 2 Color: 1
Card: 12 Suit: 0 Color: 0 Card: 12 Suit: 2 Color: 1
                         Card: 0
                                   Suit: 3
                                           Color: 1
Card: 0 Suit: 1 Color: 0
                          Card:
        Suit: 1 Color: 0
                                   Suit: 3
                                           Color:
                                 1
Card: 1
Card: 2 Suit: 1 Color: 0
                          Card:
                                2 Suit: 3 Color: 1
                          Card: 3 Suit: 3 Color: 1
         Suit: 1
                Color: 0
Card: 3
                         Card: 4 Suit: 3 Color: 1
                Color: 0
Card: 4
         Suit: 1
     5
         Suit: 1
                Color: 0
                         Card: 5 Suit: 3 Color: 1
Card:
Card: 6 Suit: 1 Color: 0
                         Card: 6 Suit: 3 Color: 1
Card: 7 Suit: 1 Color: 0 Card: 7 Suit: 3 Color: 1
Card: 8 Suit: 1 Color: 0 Card: 8 Suit: 3 Color: 1
Card: 9 Suit: 1 Color: 0 Card: 9
                                   Suit: 3 Color: 1
Card: 10 Suit: 1 Color: 0
                          Card: 10 Suit: 3
                                           Color: 1
Card: 11 Suit: 1 Color: 0
                         Card: 11
                                   Suit: 3
                                            Color: 1
                          Card: 12
                                    Suit: 3
                                           Color: 1
Card: 12 Suit: 1 Color: 0
```

Fig. 16.15 Output of the program in Fig. 16.14.

It is possible to specify an *unnamed bit field* in which case the field is used as *padding* in the structure. For example, the structure definition uses an unnamed 3-bit field as padding—nothing can be stored in those three bits. Member **b** (on our 2-byte word computer) is stored in another storage unit.

```
struct Example {
  unsigned a : 13;
  unsigned : 3;
  unsigned b : 4;
};
```

An unnamed bit field with a zero width is used to align the next bit field on a new storage unit boundary. For example, the structure definition

```
struct Example {
  unsigned a : 13;
  unsigned : 0;
  unsigned b : 4;
};
```

uses an unnamed 0-bit field to skip the remaining bits (as many as there are) of the storage unit in which a is stored, and align b on the next storage unit boundary.



Portability Tip 16.5

Bit field manipulations are machine dependent. For example, some computers allow bit fields to cross word boundaries, whereas others do not.



Common Programming Error 16.8

Attempting to access individual bits of a bit field as if they were elements of an array. Bit fields are not "arrays of bits."



Common Programming Error 16.9

Attempting to take the address of a bit field (the ϵ operator may not be used with bit fields because they do not have addresses).



Performance Tip 16.3

Although bit fields save space, using them can cause the compiler to generate slower-executing machine language code. This occurs because it takes extra machine language operations to access only portions of an addressable storage unit. This is one of many examples of the kinds of space-time trade-offs that occur in computer science.

16.9 Character Handling Library

Most data is entered into computers as characters—including letters, digits, and various special symbols. In this section, we discuss C++'s capabilities for examining and manipulating individual characters. In the remainder of the chapter, we continue the discussion of character string manipulation that we began in Chapter 5.

The character handling library includes several functions that perform useful tests and manipulations of character data. Each function receives a character—represented as an int—or EOF as an argument. Characters are often manipulated as integers. Remember that EOF normally has the value -1 and some hardware architectures do not allow negative values to be stored in char variables. Therefore, the character handling functions manipulate characters as integers. Figure 16.16 summarizes the functions of the character handling library. When using functions from the character handling library, be sure to include the <ctype.h> header file.

Prototype	Description
<pre>int isdigit(int c) int isalpha(int c) int isalnum(int c) int isxdigit(int c) int islower(int c) int isupper(int c)</pre>	Returns true if c is a digit, and false otherwise. Returns true if c is a letter, and false otherwise. Returns true if c is a digit or a letter, and false otherwise. Returns true if c is a hexadecimal digit character, and false otherwise. (See Appendix E, "Number Systems," for a detailed explanation of binary numbers, octal numbers, decimal numbers and hexadecimal numbers.) Returns true if c is a lowercase letter, and false otherwise. Returns true if c is an uppercase letter; false otherwise.

Fig. 16.16 Summary of the character handling library functions (part 1 of 2).