

$$f(n) \leq c g(n), \exists c, \epsilon n_0$$

$$\underbrace{2n^2}_f \leq c \cdot \underbrace{n^3}_g$$

$$2n^2 \leq cn^3 \Rightarrow 2 \leq cn$$

$c = 2$
$n_0 = 1$

$$n^2 = O(n^2)$$

$$\cancel{n^2} \leq c \cdot \cancel{n^2} \Rightarrow$$

$$1 \leq c$$

$c = 1$
$n_0 = 1$

$$1000n^2 + 1000n = O(n^2)$$

$$f \leq c \cdot n^2$$

f $1000n^2 + 1000n \leq 1000n^2 + 1000n^2$

$= 2000n^2$
c g

$$C = 2000$$
$$n_0 = 1$$

$$c \cdot g(n) \leq f(n)$$

$$\underbrace{5n^2}_{f} = \underbrace{\Omega(n)}_g$$

$$c \cdot n \leq 5n^2 \Rightarrow c \leq 5n$$

$c = 1$
$n_0 = 1$

$$100n + 5 \neq \Omega(n^2)$$

$$\exists c, n_0 \quad 0 \leq \underbrace{cn^2}_{\text{red box}} \leq \underbrace{100n + 5}_{\text{red box}}$$

$$100n + 5 \leq 100n + \underbrace{5n}_{\text{red box}} = \underbrace{105n}_{\text{red box}}$$

$$cn^2 \leq 105n$$

$$cn^2 - 105n \leq 0$$

$$n(cn - 105) \leq 0 \Rightarrow cn - 105 \leq 0$$

$$\Rightarrow n \leq \frac{105}{c}$$

$$\frac{n^2}{2} - \frac{n}{2} = \Theta(n^2)$$

$$\frac{n^2}{2} - \frac{n}{2} < \frac{n^2}{2}$$

$$\begin{aligned} C_1 &= \frac{1}{2} \\ n_0 &= 1 \end{aligned}$$

$$\frac{n^2}{2} - \frac{n}{2} \geq \frac{n^2}{2} - \frac{n}{2} \cdot \frac{n}{2} = \frac{n^2}{4}$$

$$n \geq 2$$

$$\begin{aligned} C_2 &= \frac{1}{4} \\ n_0 &= 2 \end{aligned}$$

$$\begin{aligned} C_1 &= \frac{1}{2} \\ C_2 &= \frac{1}{4} \\ n_0 &= 2 \end{aligned}$$