

# Non-Parametric Statistical Background Modeling for Efficient Foreground Region Detection

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**Abstract** Most methods for foreground region detection in videos are challenged by the presence of quasi-stationary backgrounds – flickering monitors, waving tree branches, moving water surfaces or rain. Additional difficulties are caused by camera shake or by the presence of moving objects in every image. The contribution of this paper is to propose a scene-independent and non-parametric modeling technique which covers most of the above scenarios. First, an adaptive statistical method, called adaptive kernel density estimation (AKDE), is proposed as a base-line system that addresses the scene dependence issue. After investigating its performance we introduce a novel general statistical technique, called recursive modeling (RM). The RM overcomes the weaknesses of the AKDE in modeling slow changes in the background. The performance of the RM is evaluated asymptotically and compared with the base-line system (AKDE). A wide range of quantitative and qualitative experiments is performed to compare the proposed RM with the base-line system and existing algorithms. Finally, a comparison of various background modeling systems is presented as well as a discussion on the suitability of each technique for different scenarios.

**Keywords** Non-Parametric Density Estimation · Recursive Modeling · Background Subtraction · Background Modeling · Quasi-Stationary Backgrounds

## 1 Introduction

Typically, in most visual surveillance systems static cameras are used. However, because of inherent changes in the background, such as fluctuations in monitors and fluorescent lights, waving flags and trees, water surfaces, etc. the background may not be completely stationary. Furthermore, the background may not appear completely empty in any image across the video sequence, thus making the background modeling even more problematic. These difficult situations are illustrated in Fig. 1. We refer to these backgrounds as quasi-stationary.



**Fig. 1** Examples of challenges in quasi-stationary backgrounds: (a) Fluctuating monitors. (b) Rain/Snow. (c) Waving tree branches. (d) Non-empty background.

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### 1.1 Related work

In the presence of quasi-stationary backgrounds a single background frame is not enough to accurately detect foreground regions. Pless *et al.* [21] evaluated different models for dynamic backgrounds. Depending on the

complexity of the problem the background models employ expected pixel features (i.e. colors) [3], [4], [5], [23], consistent motion [20], [33], or fusion of color/contrast and motion [1]. They also may employ pixel-wise information [32] or regional models of features [31], [7] and [15]. To improve robustness to noise, spatial [19] or spatio-temporal [14] features may be used.

In [32] a single 3-D Gaussian model for each pixel is built and the mean and covariance of the model are learned in each frame. This system models the noise and uses a background subtraction technique to detect those pixels whose probabilities are smaller than a heuristically selected threshold. However, the system failed to label a pixel as foreground or background when it has more than one modality due to fluctuations in its values, such as in a fluctuating monitor.

Kalman filtering [12], [9], [10] is also used to update the model and linear prediction using Wiener filtering is presented in [31]. These background models were also unable to represent multi-modal situations.

Indupalli *et al.* in [8] applied a histogram based method and a clustering technique to segment the background of the video. They also used the HSV color space in their pixel-wise system. However, their system requires that its parameters be selected manually. Also, this method fails if the scene does not have an empty background or is crowded.

In [30] Totozafiny *et al.* proposed a background segmentation system for road surveillance applications. Their technique generates the background model using a background reference frame and a mixture of Gaussians. This method is not adaptive to gradual and local changes in the illumination of the scene since it generates the model only once. The system is not scene independent and its parameters should be updated from application to application.

A mixture of Gaussians modeling technique was proposed in [25], [24] and [6] to address the multi-modality of the underlying background. In this technique background pixels are modeled by a mixture of Gaussians. During the training stage, parameters and weights of the Gaussians are trained and used in the background subtraction where the probability of each pixel is generated using the mixture of Gaussians. The pixel is labeled as foreground or background based on its probability.

There are several shortcomings for mixture learning methods. First, the number of Gaussians needs to be specified. Second, this method does not explicitly handle spatial dependencies. Even with the use of incremental expectation maximization, the parameter estimation and its convergence is noticeably slow where the Gaussians adapt to a new cluster. The convergence

speed can be improved by sacrificing memory as proposed in [16] and [17], limiting its applications when mixture modeling is pixel-based and over long temporal windows.

A recursive filter formulation is proposed by Lee in [13] to speed up the convergence. However, the problem of specifying the number of Gaussians as well as the adaptation in later stages still exists. This model does not account for situations in which the number of Gaussians changes due to occlusion or uncovered parts of the background.

In [5], El Gammal *et al.* proposed a non-parametric kernel density estimation method (KDE) for pixel-wise background modeling without making any assumption about its probability distribution. Therefore, this method can easily deal with multi-modality in background pixel distributions without specifying the number of modes in the background. However, there are several issues to be addressed using non-parametric kernel density estimation.

These methods are memory and time consuming since for each pixel in each frame the system has to compute the average of all kernels centered at each training sample. The size of temporal window used as the background model needs to be specified. Too small a window increases speed, while it does not incorporate enough history for the pixel, resulting in a less accurate model. The adaptation will be problematic by using small window sizes. Increasing the window size improves the model accuracy but at the cost of higher memory requirements and slower convergence. In order to adapt the model a sliding window is used in [18]. However, the model convergence is problematic in situations where the illumination suddenly changes.

In order to update the background for scene changes such as moved objects, parked vehicles or opened/closed doors, Kim *et al.* in [11] proposed a layered modeling technique. This technique needs an additional model called *cache* and assumes that the background modeling is performed over a long period of time. It should also be used as a post-processing stage after the background is modeled.

Another approach to model variations in the background is to represent these changes as different states corresponding to different environments – such as lights on/off, night/day, sunny/cloudy. For this purpose Hidden Markov Models (HMM) have been used in [22] and [26]. However, these techniques suffer from slow model training speed and are sensitive to model selection and initialization.

## 1.2 Motivation and contributions

Because of the aforementioned issues in detecting foreground regions in videos with quasi-stationary backgrounds existing systems addresses some of these problems in a specific or a combination of scenarios. Our focus here is to find a common ground that would cover a general scenario for background modeling. Contributions of this study can be summarized as follows:

- Finding an appropriate approach to the problem of detecting foreground regions in videos with quasi-stationary background. This approach should address the multi-modality of the background as well as scene-independence. Our proposed solution is based on a non-parametric framework that addresses the issues in the literature. This base-line system, called Adaptive Kernel Density Estimation (AKDE), outperforms the existing methods in the literature [27], [28].
- Investigating the efficiency of the base-line system and deriving a more universal framework upon this system. The proposed general method is called Recursive Modeling (RM). This technique addresses the issue of robust background training in slowly changing backgrounds, non-empty backgrounds, and backgrounds with steady, irregular global motion (hand-held camera).

**The AKDE.** The theory behind the AKDE algorithm is to estimate the probability of each pixel being background based on a number of samples in its history. One advantage of the AKDE method over existing kernel density estimation modeling is in using a different threshold for each pixel, instead of a single threshold for all pixels in the scene. These thresholds are independently trained over a number of video frames.

By training the thresholds the system becomes scene independent and there is no need to heuristically select and tune threshold values in different scenes. By employing these localized thresholds the system works efficiently on different video scenes and is more robust to local changes in the same scene. The proposed AKDE method exploits the dependency between pixel color components as well, thus leading to a more accurate background model.

**The RM.** The RM method is a recursive counterpart for the AKDE technique which uses pixel intensity/color values in new frames to update the background model at that pixel location. Since the update process is performed continuously, the background model converges to the actual one as more frames emerge and are processed. This gives the RM its ability to detect foreground regions when the background changes occur slowly and do not fit in a small temporal window.

In videos without a set of empty background frames the proposed RM technique has the ability to generate a clear background model because pixels belonging to the actual background provide more support for the background model.

In order to make the background model converge to the actual one and recover from the expired model faster the proposed RM method uses a schedule for learning. It should be noticed that a non-parametric recursive modeling scheme has not been investigated in the literature.

The rest of the paper is structured as follows. Section 2 presents the base-line AKDE method and evaluates its performance and efficiency. This system and a benchmark data provide a standard set of comparison tests. Section 3 present the proposed RM technique and an evaluation of its performance with regard to the standard assessment presented for the base-line system. In section 5, a comprehensive comparison between these two methods and other techniques is conducted and the situations in which each of the proposed methods is superior are presented. Finally, section 6 concludes the paper and gives future directions of the research.

## 2 Adaptive kernel density estimation (AKDE)

In this section we present a novel technique for background modeling based on adaptive non-parametric kernel density estimation (AKDE) [28].

### 2.1 The algorithm

Fig. 2 shows the pseudo-code for the AKDE algorithm, consisting of three major stages: training, classification and update. In the training stage the background model is generated, and for each pixel its model values are used to estimate the probability of that pixel to be background in new frames. The proposed method detects foreground regions by solving a classification problem. However, it should be noted that we only have samples of the background class before any foreground object appears in the scene.

The only parameter in kernel density estimation is the kernel bandwidth. In theory, as the number of training samples grows without a bound the estimated density converges to the actual underlying density regardless of the kernel bandwidth value [2].

### 2.2 Non-parametric density estimation

In the proposed AKDE method a non-parametric model for each pixel is generated and its classifier is trained.

```

N: size of training buffer
For each frame at time t
1. Training stage
  for each pixel (u,v)
    - Calculate kernel covariance  $\Sigma(u,v)$  and threshold  $th(u,v)$ .
2. Classification stage
  for each pixel (u,v)
    - Compute median of estimated probability in its neighborhood:  $Med(u,v)$ 
    - if  $Med(u,v) \leq th(u,v)$ 
      then  $FG_t(u,v) = 1$  % (Foreground)
      else  $FG_t(u,v) = 0$  % (Backgrounds)
3. Update stage
  - if  $size(FG) \geq 0.5 \text{ Image\_Size}$ 
    then
      for each pixel (u,v)
         $OF(u,v) \leftarrow I_t(u,v)$ 
      else
        for each pixel (u,v)
           $OF(u,v|FG_t(u,v) = 0) \leftarrow I_t(u,v|FG_t(u,v) = 0)$ 
    % Global sudden change detected
    % Replace oldest frame (OF)
    % with current frame
    % Gradual change
    % Replace background pixels in OF
    % with those in current frame

```

Fig. 2 The proposed AKDE modeling algorithm.

It uses the history of pixel values as training samples and estimates the probability of each pixel being background in new frames as the classification criterion. In the classification stage each pixel is classified as foreground or background based on its estimated probability, computed by:

$$P_t(\mathbf{x}_t) = \frac{1}{N2\pi|\Sigma|^{1/2}} \sum_{i=1}^N e^{-\frac{1}{2}(\mathbf{x}_t - \mathbf{x}_i)^T \Sigma^{-1}(\mathbf{x}_t - \mathbf{x}_i)} \quad (1)$$

where  $\mathbf{x}_t$  is the pixel feature vector at time  $t$  and  $\mathbf{x}_i$  are its values in the training sequence.  $\Sigma$  is a positive definite symmetric matrix which is the kernel bandwidth matrix and  $N$  is the number of frames used to train the background model. In order to capture dependencies between features for each pixel,  $\Sigma$  has to be a full (non-diagonal) matrix.

Since in the AKDE method no assumptions are made on the covariance matrix  $\Sigma$ , any features for each pixel can be used. Because color is the easiest and most reliable feature to extract we use chrominance values for each pixel. That is, given color values in  $RGB$  space we determine red ( $c_r$ ) and green ( $c_g$ ) chrominance values by:

$$\begin{aligned} c_r &= \frac{R}{R+G+B} \\ c_g &= \frac{G}{R+G+B} \end{aligned} \quad (2)$$

Therefore the feature vector for each pixel at a given time  $t$  is defined by:

$$\mathbf{x}_t = [c_r(t), c_g(t)]^T \quad (3)$$

Due to limited memory and computational power, we need to store a rather short term memory of the

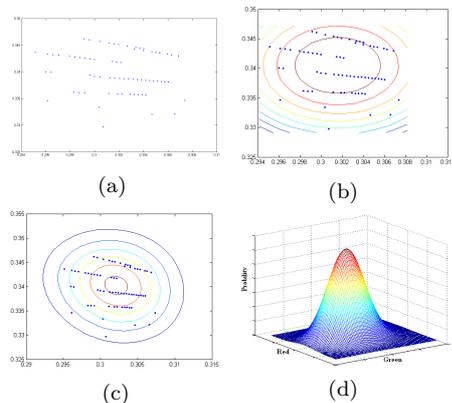


Fig. 3 Diagonal vs full kernel matrix: (a) Pixel chrominance scatter plot ( $c_r, c_g$ ) for one pixel over time. (b) Probability constant contours using diagonal covariance matrix. (c) Probability constant contours using full covariance matrix. (d) Probability density using full covariance matrix.

background frames as training samples. This makes the non-parametric kernel density estimation dependent on the choice of its kernel bandwidth. In order to achieve an accurate and automatic background model, which is adaptive to the spatial information in the scene, the kernel bandwidth matrix needs to be trained.

The effect of using a full covariance matrix can be observed in Fig. 3. By using a full covariance matrix ( $\Sigma$ ) in equation (1) we do not impose an assumption of feature independence on our estimation. If we assumed that features for each pixel are independent then a simplified version of equation (1) could be used, where the covariance matrix is diagonal. However, as it can be seen from Fig. 3 by using chrominance features, the independence assumption is not valid and the full covariance matrix results in a more accurate density es-

timation, as opposed to the diagonal covariance matrix proposed in [5].

### 2.3 Training stage

For each pixel the training samples are vectors  $\mathbf{X}_N = \{\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N\}$ , where  $N$  is the number of training frames. In our experiments we chose  $N = 300$  for most of the scenes. The successive deviation of the above vectors is a matrix  $\Delta_X$  whose columns are:

$$[\mathbf{x}_i - \mathbf{x}_{i-1}]^T \quad \text{with } i = 2, 3, \dots, N \quad (4)$$

For each pixel, the kernel bandwidth matrix is defined such that it represents the temporal scatter of training samples. Thus the kernel bandwidth is:

$$\Sigma = \text{cov}(\Delta_X) \quad (5)$$

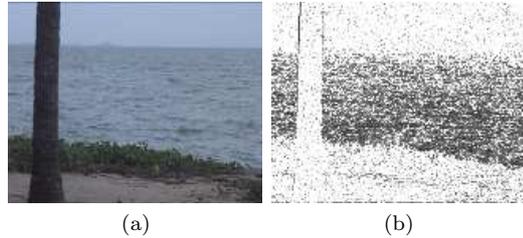
From equations (4) and (5) it can be seen that for pixels with more feature changes through time, such as flickering pixels, the kernel bandwidth matrix has larger elements, while for pixels that do not change much its elements are smaller. Also notice that the kernel bandwidth is drawn from the training samples without any assumption on features and their underlying probability density function. The estimated probability density function by using this adaptive kernel bandwidth is accurate, even with a small number of background training frames. Finally, since the kernel bandwidth matrix is computed using successive deviations in equation (4) it accounts for temporal dependencies in pixel feature vectors.

In the traditional foreground detection techniques, usually the foreground regions are detected by comparing the value or model of each pixel with its value or model in the background. If this deviation is larger than a heuristically selected threshold it is labeled as a foreground region. If we estimate the probability of each pixel in all of the background frames, given that all pixels are background, their probabilities should have large values, close to 1. But because of noise and inherent background changes, pixels do not take a single value and their probabilities become smaller. The probability of a pixel to be background is related to the amount of change that its features undergo in time. Therefore a single global threshold does not work well because pixels in different locations undergo different amounts of change.

These threshold values need to be trained for each pixel during the training stage to build an accurate and automatic classifier. For each pixel its threshold value ( $th$ ) is selected such that its classifier results in 5% false

reject rate. That is, 95% of the time the pixel is correctly classified as belonging to background:

$$\sum_{\substack{i=1 \\ P(Bg|x_i) \leq th}}^N P(Bg|x_i) \leq 0.05 \sum_{i=1}^N P(Bg|x_i) \quad (6)$$



**Fig. 4** Adaptive threshold map: (a) An arbitrary frame. (b) Threshold map.

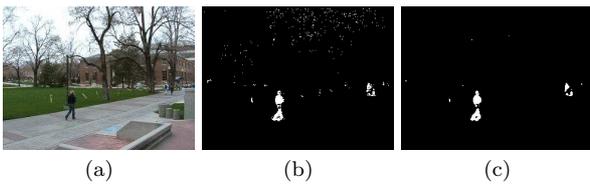
This can be seen in Fig. 4, where (a) shows an arbitrary frame of a sequence containing a water surface and (b) shows the trained threshold map for this frame. Darker pixels in Fig. 4(b) represent smaller threshold values and lighter pixels correspond to larger threshold values. The thresholds in areas that tend to change more, such as the water surface, are lower than those in areas with less amount of change, such as the sky. Since the probability density function is normalized, for pixels which undergo more changes the estimated probability density function is wider. As a result, in order to keep 5% false reject rate, smaller threshold values are needed. Note that the threshold map is noisy, since for efficiency purposes only 150 frames are used.

### 2.4 Classification stage

In the training stage, for each pixel its kernel bandwidth matrix  $\Sigma$  and its classification decision criterion  $th$  were determined. The probability of each pixel in the new frame is then estimated using equation (1). If we directly apply the trained threshold of each pixel to its estimated probability, due to impulse noise isolated pixels may still be erroneously classified.

One of the properties of this type of noise is that, if strong noise affects a pixel, it is less likely to affect its neighbors with the same strength. If a pixel in a region belonging to the background produces a fairly small probability because of noise, its neighboring pixels are expected to produce larger probabilities.

Notice that this impulsive noise is introduced to the system as a byproduct of the probability density estimation. As known, median filtering is a suitable tool to remove this type of noise. Applying the median filtering directly to the images suppresses the impulsive



**Fig. 5** Enforcing spatial consistency: (a) Original frame (b) Detected foreground regions by applying thresholds directly on the estimated probability. (c) Detected foreground regions by applying threshold on median of probabilities in a neighborhood.

noise in the frames but does not significantly affect the noise introduced by the process. In order to remove the process noise we apply the median of estimated probabilities in a region around a pixel. After estimating the probability of each pixel in the new frame, the median of probabilities in its 8-connected neighborhood is compared with its threshold to make the classification decision:

$$\text{Label}_t = \begin{cases} \text{Foreground} & \text{if } \text{median}(\text{Prob}_t) \leq th \\ \text{Background} & \text{otherwise} \end{cases} \quad (7)$$

Fig. 5 shows the effect of enforcing spatial consistency using the median of probabilities in foreground region detection. As it can be seen, by applying the threshold on the median of estimated probabilities of pixels in a neighborhood, most of the noise can be suppressed, while maintaining the image quality.

### 2.5 Update stage

In the proposed AKDE method we use two different types of adaptation. To make the system adaptive to *gradual changes* in illumination, we replace the pixels in the oldest background frame with those belonging to the current background mask. In order to detect *sudden changes* in the illumination, the area of the foreground objects are checked. Once a *sudden change* is detected (detected foreground region is very large), the classification stage of the algorithm is suspended and new frames replace all frames in the background training buffer.

Because the training stage of the algorithm is time consuming, the updating stage is actually performed every few frames, depending on the rate of changes and the processing power. In the current implementation the updating stage is performed every 100-150 frames.

## 3 Recursive modeling (RM)

In this section we describe our novel recursive method. The formulation is discussed in one dimension and its extension to higher dimensions is straightforward. We

explain how dependencies between pixel features in higher dimensions can be captured, resulting in more accurate models.

### 3.1 The algorithm

The proposed method, in pseudo-code, is shown in Figure 6.  $\theta_t^B$  is the background model and  $\theta_t^F$  is the foreground model for each pixel. Let  $x_t$  be the intensity value of a pixel at time  $t$ . The non-parametric estimation of the background model that accurately follows its multi-modal distribution can be reformulated in terms of recursive filtering [29]:

$$\hat{\theta}_t^B(x) = [1 - \beta_t] \cdot \theta_{t-1}^B(x) + \alpha_t \cdot H_\Delta(x - x_t) \quad (8)$$

$$\sum_{x=0}^{255} \theta_t^B(x) = 1 \quad (9)$$

where  $x \in [0, 255]$  and  $\theta_t^B$  is the background pixel model at time  $t$ , normalized according to (9).  $\hat{\theta}_t^B$  is updated by the local kernel  $H(\cdot)$  with bandwidth  $\Delta$  centered at  $x_t$ . Parameters  $\alpha_t$  and  $\beta_t$  are the learning rate and forgetting rate schedules, respectively. The kernel  $H$  should satisfy the following conditions:

$$\begin{aligned} \sum_x H_\Delta(x) &= 1 \\ \sum_x x \times H_\Delta(x) &= 0 \end{aligned} \quad (10)$$

These conditions should be satisfied to ensure that the kernel is normalized, symmetric and positive definite in case of multivariate kernels. In our implementation of the RM method we use a Gaussian kernel which satisfies the above conditions. Note that in this context there is no need to specify the number of modalities of the background representation at each pixel.

Fig. 7 shows the updating process using our proposed recursive modeling technique. It can be seen that the trained model (solid line) converges to the actual one (dashed line) as new samples are introduced. The actual model is the probability density function of a randomly generated sample population and the trained model is generated by using the recursive formula presented in (8).

In existing non-parametric kernel density estimation methods the learning rate  $\alpha$  is selected to be constant and has small values. This makes the pixel model convergence slow and keeps its history in the recent temporal window of size  $L = 1/\alpha$ . The window size in non-parametric models is important as the system has to cover possible fluctuations in the background model.

1. Initialization:  $\Delta$ ,  $\alpha_0$ ,  $\beta$ ,  $\kappa$  and  $th$
2. For each frame at time  $t$ 
  - For each pixel
    - 2.1. Training stage
      - Update  $\alpha_t = \frac{1-\alpha_0}{h(t)} + \alpha_0$  and  $\Delta$
      - Update  $\theta_t^B(x) = (1-\beta_t)\theta_{t-1}^B(x) + \alpha_t \cdot H_\Delta(x-x_t)$
      - If  $\theta_t^B \leq th$  then update  $\theta_t^F(x) = (1-\beta_t)\theta_{t-1}^F(x) + \alpha_t \cdot H_\Delta(x-x_t)$
    - 2.2. Classification stage
      - If  $\ln(\text{med}(\theta_t^B)/\text{med}(\theta_t^F)) \leq \kappa$  then label pixel as foreground.
    - 2.3. Update stage
      - Update  $\kappa$  and  $th$

Fig. 6 Our proposed RM algorithm.

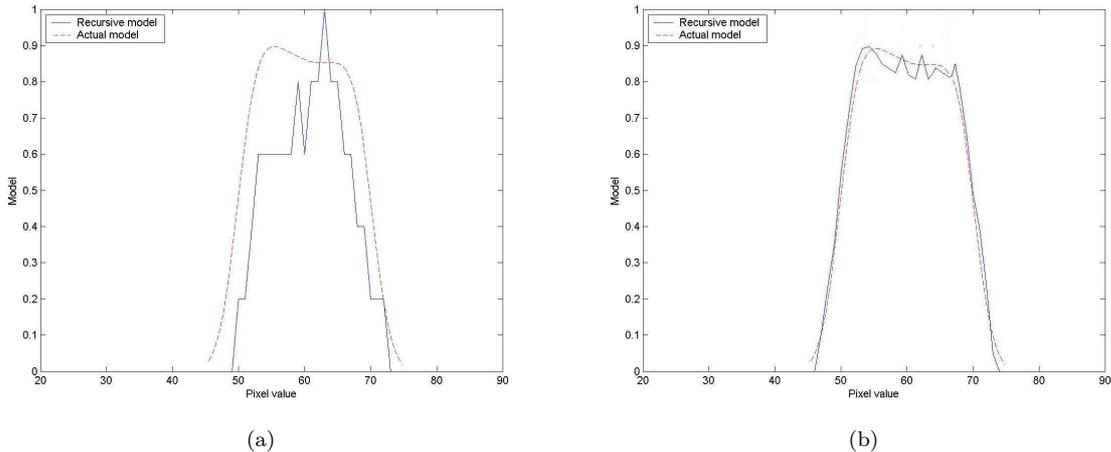


Fig. 7 Recursive modeling: Model after (a) 10 frames. (b) 200 frames.

That is, pixel intensity changes may not be periodic or regular and consequently may not fit in a small temporal window. In such cases larger windows are needed, resulting in higher memory and computational requirements. Another issue in non-parametric density estimation techniques is that the window size is fixed and the same for all pixels in the scene. However, some pixels may have fewer fluctuations and therefore need smaller windows to be accurately modeled, while others may need a much longer history to cover their changes.

### 3.2 Scheduled learning

In order to speed up the modeling convergence and recovery we use a schedule for learning the background model at each pixel based on its history. This schedule makes the adaptive learning process converge faster, without compromising the stability and memory requirements of the system. The learning rate changes according to the schedule:

$$\alpha_t = \frac{1 - \alpha_0}{h(t)} + \alpha_0 \quad (11)$$

where  $\alpha_t$  is the learning rate at time  $t$  and  $\alpha_0$  is a small target rate which is:

$$\alpha_0 = 1/256 \times \sigma_\theta \quad (12)$$

where  $\sigma_\theta$  is the model variance. The function  $h(t)$  is a monotonically increasing function:

$$h(t) = t - t_0 + 1 \quad (13)$$

where  $t_0$  is the time at which a sudden global change is detected. At early stages the learning occurs faster ( $\alpha_t = 1$ ) and monotonically decreases to converge to the target rate ( $\alpha_t \rightarrow \alpha_0$ ). When a global change is detected  $h(t)$  resets to 1. Later in section 5 we discuss the effect of this schedule on improving the convergence and recovery speed.

The forgetting rate schedule is used to account for removing the values that have occurred a long time ago and no longer exist in the background. In the current implementation we assume that the forgetting rate is a portion of the learning rate  $\beta_t = l \cdot \alpha_t$ , where  $l = 0.5$ .

### 3.3 Training stage

Before new objects appear in the scene, at each pixel all the intensity values have the same probability of be-

ing foreground. However, in each new frame the background models are updated according to equation (8), resulting in larger model values ( $\theta^B$ ) at the pixel intensity value  $x_t$ . In essence the value of background pixel model at each intensity  $x$  is:

$$\theta_t^B(x) = P(\text{Bg}|x) \quad x \in [0, 255] \quad (14)$$

In order to achieve better detection accuracy, we introduce the foreground model. Later in the classification stage the foreground model is compared to the background model. For all  $x \in [0, 255]$ , the foreground model is defined by:

$$\hat{\theta}_t^F(x) = [1 - \beta_t^F] \cdot \theta_{t-1}^F(x) + \alpha_t^F \cdot H_\Delta(x - x_t) \quad (15)$$

$$\sum_{x=0}^{255} \theta_t^F(x) = 1 \quad (16)$$

Once the background model is updated for each pixel, it is compared to the threshold  $th$ . If its value is less than this threshold the foreground model for that pixel value is updated according to (15) and (16).

### 3.4 Classification stage

For each pixel at time  $t$  we use a function  $\theta_t^B$  for the background model and  $\theta_t^F$  for the foreground. The domain of these functions is  $[0, 255]^N$ , where  $N$  is the dimensionality of the pixel feature vector. For simplicity assume the one dimensional case again, where  $\theta_t$  is the background/foreground model whose domain is  $[0, 255]$ . From equation (15), each model ranges between 0 to 1 and its value shows the amount of evidence accumulated in the updating process (i.e., the estimated probability). For each new intensity value  $x_t$  we have the evidence of each model as  $\theta_t^B(x_t)$  and  $\theta_t^F(x_t)$ . The classification uses a *maximum a posteriori* criterion to label the pixel as foreground:

$$\ln \left( \frac{\theta_t^B}{\theta_t^F} \right) \leq \kappa \quad (17)$$

### 3.5 Updating stage

In many applications with dynamic or quasi-stationary backgrounds, we need adaptive classification criteria. Because not all pixels in the scene follow the same changes, the decision threshold  $\kappa$  should be adaptive and independent for each pixel and has to be driven from the history of that pixel. Fig. 4 explains this issue. The argument is similar to issue the of adaptive, localized threshold map discussed in section 2.2.

From the algorithm shown in Fig. 6 it can be observed that there are two set of thresholds  $th$  and  $\kappa$ .

Thresholds  $th$  for each pixel should adapt to a value where:

$$\sum_{\theta_t^B(x) \geq th} \theta_t^B(x) \geq 0.95 \quad (18)$$

For the other set of thresholds  $\kappa$ , we similarly use a measure of changes in the intensity at each pixel position. Therefore the threshold  $\kappa$  is inversely proportional to the background model variance:

$$\kappa \approx \ln \left\{ \left[ \sum_{x=0}^{255} (\theta_t^B(x) - \text{mean}[\theta^B(x)])^2 \right]^{-1} \right\} \quad (19)$$

This ensures that for pixels with more changes, smaller threshold values are chosen for classification, while for those pixels with fewer changes larger thresholds are employed. It should be mentioned that in the current implementation of the algorithm, the thresholds are updated every 30 frames.

### 3.6 Incorporating color information

In the above section we described the recursive learning scheme in 1-D where the background and foreground models are updated using the intensity value of pixels at each frame. To extend the modeling in higher dimensions and incorporate color information, one may consider each pixel as a 3 dimensional feature vector in  $[0, 255]^3$ . The kernel  $H$  in this space is a multivariate kernel  $H_\Sigma$ . In this case, instead of using a diagonal matrix  $H_\Sigma$  a full multivariate kernel can be used. The kernel bandwidth matrix  $\Sigma$  is a symmetric positive definite  $3 \times 3$  matrix. Given  $N$  pixels,  $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N$ , labeled as background, their successive deviation matrix is a matrix  $\Delta_X$  whose columns are:

$$[\mathbf{x}_i - \mathbf{x}_{i-1}]^T \quad \text{with } i = 2, 3, \dots, N \quad (20)$$

The bandwidth matrix is defined such that it represents the temporal scatter of training samples:

$$\Sigma = \text{cov}(\Delta_X) \quad (21)$$

However, in the current implementation only red and green chrominance values are used. Also in order to decrease the memory requirements of the system we assumed that the two chrominance values are independent. Making this assumption results in a significant decrease in memory requirements while the accuracy of the model does not decay drastically. The red/green chrominance values are quantized into 256 discrete values.

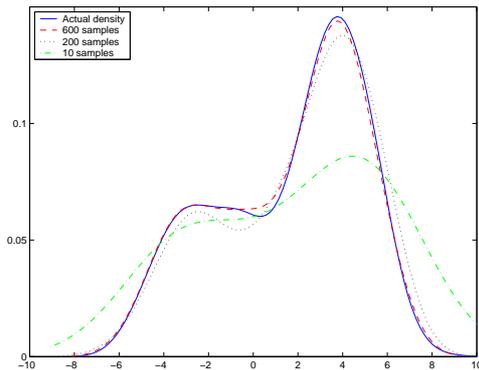


Fig. 8 Effect of the number of training samples on the estimated density function.

## 4 Performance evaluation

In this section we evaluate the performance of each of the proposed methods separately. The evaluation is conducted in terms of the number of system parameters, their impact on the output of the system, memory requirements and accuracy of the results.

### 4.1 Adaptive kernel density estimation method (AKDE)

In this section we present the system details and analyze its performance.

**Parameters.** One important parameter in this method is the number of training samples used to estimate the probability density. Other parameters such as the threshold and the kernel bandwidth matrix are trained during the training stage. In Fig. 8 the actual probability function of a randomly distributed population is shown by the solid line. The estimated probability density function converges to the underlying density by increasing the number of training samples. However, there is a trade-off between the number of training samples, memory requirements and convergence speed of the algorithm.

**Memory requirements.** The system needs to store all the training samples in order to estimate the probability of a new sample. If only pixel intensity values are to be employed for each pixel,  $n$  values should be stored. Given that these values range is between 0 to 255, each intensity value is stored in 1 byte, resulting in  $n$  bytes per-pixel memory requirement. Also the system needs to store the kernel bandwidth and the thresholds for each pixel, which result in 2 floating numbers. Considering that each floating number can be stored in 4 bytes, 8 bytes per pixel are needed to store the kernel bandwidth and the threshold. This results in  $n + 8$

bytes memory requirement per pixel. Similarly, the per-pixel memory requirements using chrominance values are  $8n + 20$ .

From the above discussion we can conclude that the asymptotic memory requirement for the system is  $O(n)$ . That is, if the number of training samples reaches infinity the memory requirements of the system grow linearly.

**Computational cost.** If we only use pixel intensity values for  $n$  training samples per pixel we need 2 additions and 2 multiplications for each training sample. This results in  $2n$  addition and  $2n$  multiplication operations. Given the optimal implementation of the exponential function using look-up tables, its cost is equal to a memory indexing. This can be assimilated to a single addition operation. The per-pixel computational cost of the AKDE method is  $5 \times n$ . If chrominance values are used the computational cost will be  $13 \times n$  per pixel.

Given the optimal implementation of the exponential function and multiplication operations, the asymptotic per-pixel computational cost is  $O(n)$ . Note that this is the optimal asymptotic computational cost per pixel. The actual frame rate of the current implementation of the AKDE method is about 5-10 fps.

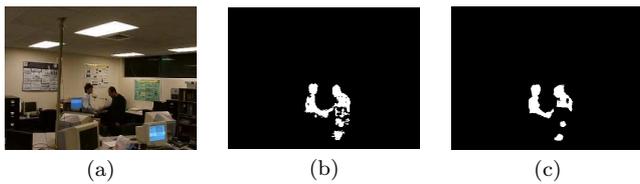
### 4.2 Recursive modeling method (RM)

In this section we analyze the performance of our recursive modeling method.

**Parameters.** In the RM method there are 5 parameters: the learning and forgetting rate  $\alpha$  and  $\beta$ , thresholds  $th$  and  $\kappa$ , and the bandwidth  $\Sigma$ . As described earlier, these parameters are trained and estimated from the data to generate an accurate and robust model. The reason that the RM technique is robust is in using most of the information in the data set and not being limited on the number of training samples. With all parameters being updated, the system performance does not depend on heuristically (and scene dependent) values for these parameters.

**Memory requirements.** If pixel intensity is used in the RM technique the model becomes a 1-D function representing the probability mass function of the pixel. The pixel intensity values range is from 0 to 255 making the memory requirements of the RM equal to  $256 \times 4$  bytes per pixel. Using chrominance values, the model is 2-D and needs  $256^2 \times 4$  bytes in memory.

The current implementation of the RM method uses a simple assumption of independence between color features which results in  $8 \times 256$  bytes memory requirements [29]. Color components are not independent. How-



**Fig. 9** Rapidly fluctuating background: (a) *Handshake* video sequence. (b) Detected foreground regions using AKDE. (c) Detected foreground regions using RM.

ever, assuming that they are independent helps decreasing memory needs drastically while the accuracy does not decrease significantly. In conclusion the asymptotic memory requirement of the RM algorithm is constant  $O(1)$ .

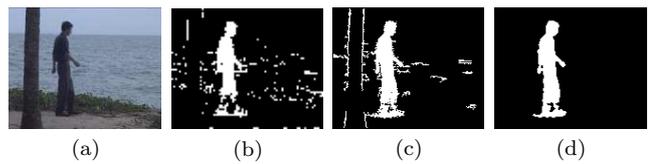
**Computational cost.** If we only use pixel intensity values for pixels we need 256 addition and  $2 \times 256$  multiplication operations. Similarly, if we use 2-D chrominance values as pixel features and using the independence assumption discussed earlier, the system requires only  $2 \times 256$  addition and  $4 \times 256$  multiplication operations to update the model.

The asymptotic computation cost for this system is constant,  $O(1)$ , since the updating process merely consists of adding two 1-D functions. Note that this technique does not need to compute the exponential function and it acts as an incremental process, updating the model at each frame using the kernel and the previous model. The algorithm is inherently fast and an efficient implementation runs in real-time reaching frame rates of 15-30 fps.

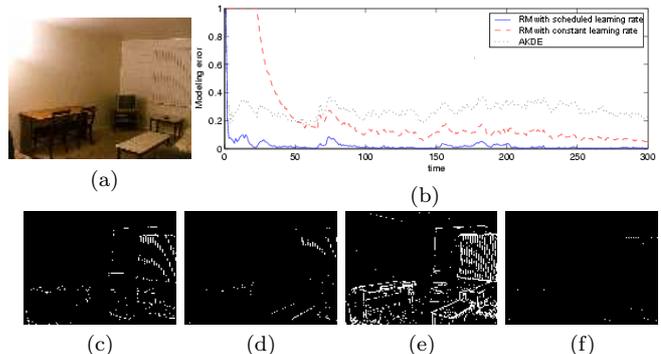
## 5 Comparison

In this section we compare the performance of proposed techniques using several real video sequences that pose significant challenges. Also their performances are compared with the mixture of Gaussians method [25], the spatio-temporal modeling presented in [14] and the simple KDE method [5]. We use different scenarios to test the performance of the proposed techniques and discuss where each method is more suitable.

**Rapidly fluctuating backgrounds.** As described above, for videos with rapidly changing background, the AKDE method has a better performance in terms of memory requirements and speed. Our experiments showed that for videos where possible fluctuations in the background occur in about 10 seconds, the AKDE technique needs less memory and works faster compared to the RM method. Fig. 9 shows the detection results of the AKDE and RM algorithms on the *Handshake* video sequence. As it can be seen from this figure, capturing dependencies between chrominance features



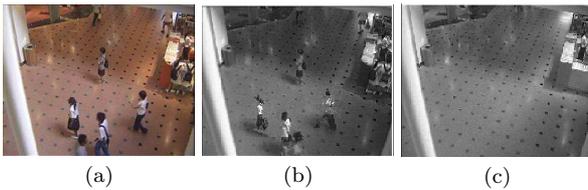
**Fig. 10** Slowly changing background: (a) *Water* video sequence. Detected foreground region using: (b) MoG. (c) AKDE. and (d) RM.



**Fig. 11** Hand-held camera: (a) *Room* video sequence. (b) Modeling error in a hand-held camera situation using different methods. (c) False positives after 2 frames using the AKDE method. (d) False positives after 247 frames using the AKDE method. (e) False positives after 2 frames using the RM method. (f) False positives after 247 frames using the RM method.

results in a more accurate foreground region (in Fig. 9(b)), showing that AKDE performs better than the RM. Note that this is a low contrast video sequence and the color of foreground objects is close to the background in some regions. Also in both methods fluctuations in monitors are completely modeled as a part of background and not detected as foreground regions.

**Slowly changing backgrounds.** For videos with slowly changing backgrounds or backgrounds in which changes are not periodic, the AKDE method needs more training frames to generate a good model for the background. This increases the system memory requirements and drastically decreases its speed. In these situations the RM technique is a very good alternative, since its performance is independent of the number of training frames. Fig. 10(a) shows an arbitrary frame of the *Water* video sequence. In this figure the detection results of both AKDE and RM methods are presented. This example is particularly difficult because waves do not follow a regular motion pattern and their motion is slow. Fig. 10(b) shows the result of the MoG [25]. As it can be seen from Fig. 10(c), using the AKDE method without any post-processing results in many false positives. Fig. 10(d) shows the detection results of the RM method, which outperforms both AKDE and MoG in the presence of slowly changing backgrounds.



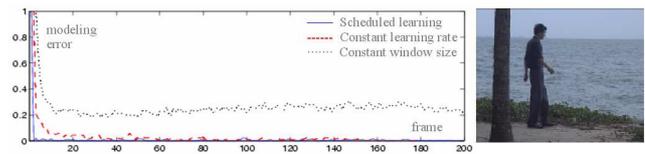
**Fig. 12** Non-empty background: (a) *Mall* video sequence. (b) Background model after 5 frames using the RM method. (c) Background model after 95 frames using the RM method.

**Hand-held camera.** In situations when the camera is not completely stationary, such as the case of a hand-held camera, the AKDE method is not suitable. In these situations there is a consistent, slow and irregular global motion in the scene, which can not be modeled by a limited size sliding window of training frames. In such cases the RM method is highly preferable.

Fig. 11 shows the modeling error of the RM method in the *Room* video sequence. In Fig. 11(a) an arbitrary frame of this video is shown. Fig. 11(b) compares the modeling error using different techniques. As it can be seen, the modeling error using a constant window size in the AKDE (the dotted line) is between 20%-40%, and it does not decrease with time. This shows that the system using the AKDE method with a constant sized sliding window never converges to the actual model. The dashed line shows the modeling error using the RM method with a constant learning rate, and the solid line shows the modeling error of the RM with scheduled learning. We conclude that the model generated by the RM technique eventually converges to the actual background model and its error goes to zero. Fig. 11(c) and (d) show misclassified regions using the AKDE method after 2 and 247 frames respectively and Fig. 11(e) and (f) show the false positives using the RM method after 2 and 247 frames into the video. As it can be seen, the amount of false positives decrease with time as the system accumulates most changes observed in the history of the scene using the RM method, but for the AKDE it does not converge to zero.

**Non-empty backgrounds.** In situations where the background of the video is not empty (there is no clear background at any time in the video sequence), the AKDE method fails to accurately detect the foreground regions. In these situations the RM technique has to be used to generate an accurate empty background model.

Fig. 12 shows the background model in the *Mall* video sequence in which the background is never empty. In this situation the AKDE method fails unless a post-processing on the detected foreground regions is performed to generate models for uncovered parts of the background. This system considers the foreground objects present in the background training window as a



**Fig. 13** Convergence speed.

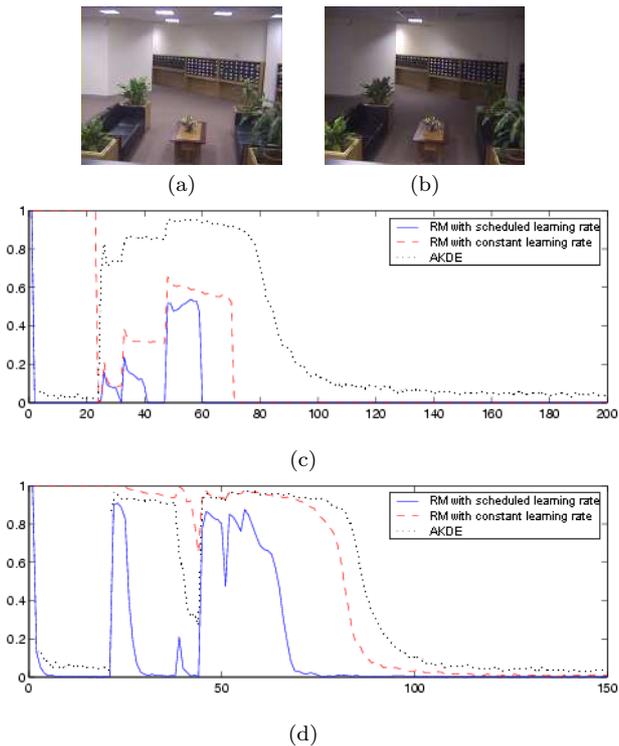
part of background. When those objects move their empty position is detected as a foreground region. In the RM method however, the background model is updated at every frame from the beginning of the video. When an object moves the new pixel information is used to update the background model to the new one. Figure 12(b) shows the background model after 5 frames from the beginning of the video and Fig. 12(c) shows the model after 95 frames.

In this scenario consistent background regions are temporarily occluded by transient moving objects. Therefore the background itself contributes more consistent information to the model. As a result, the model converges to the empty background. This can be observed from Figure 12.

**Convergence speed.** An important issue in the recursive learning is the convergence speed of the system (how fast the model converges to the actual background). Fig. 13 illustrates the convergence speed of our approach with scheduled learning, compared to constant learning and kernel density estimation with constant window size.

**Sudden global changes in the background.** In situations where the video background suddenly changes – such as lights on/off – the proposed RM technique with scheduled learning recovers faster than the AKDE method. Generally, with the same speed and memory requirements, the RM method results in faster convergence and lower model error than existing techniques.

Fig. 14 shows the comparison of the recovery speed from an expired background model to the new one. Fig. 14(a) depicts an indoor scene with lights on and Fig. 14(b) shows the scene with the lights off. In our example (Fig. 14(c)) lights go from on to off through three global but sudden changes occurring at frames 23, 31 and 47. As shown, the scheduled learning RM method (solid curve) recovers the background model after these changes faster than non-scheduled RM and the AKDE with constant window size. The constant, large learning rate recovers more slowly (dashed curve) while the AKDE technique (dotted curve) is not able to recover even after 150 frames. A similar situation with lights going from off to on through three global, sudden illumination changes is shown in Fig. 14(d). It needs to be mentioned that the mixture learning algorithms are even slower in convergence and recovery. A typical mix-



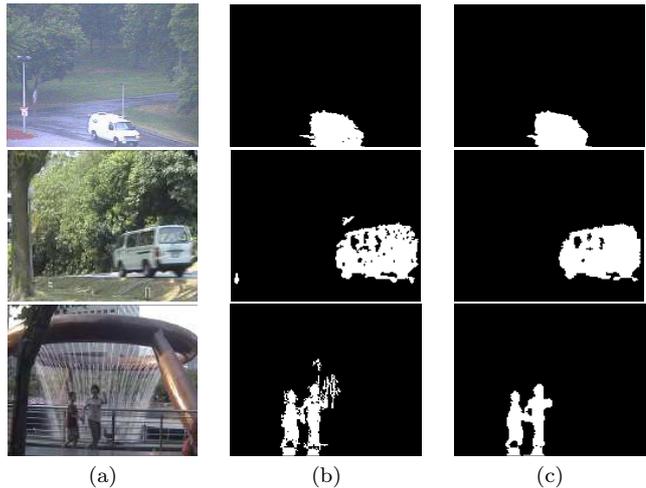
**Fig. 14** Sudden global changes in the background: (a) *Lobby* video sequence with lights on. (b) Lights off. (c) Recovery speed comparison in lights turned off scenario. (d) Recovery speed comparison in lights turned on scenario.

ture learning technique proposed in [25] needs at least 1000 frames to converge.

**Other difficult examples.** Fig. 15 shows three video sequences with challenging backgrounds. In column (a) the original frames are shown, while column (b) and (c) show the results of the AKDE and the RM methods, respectively. Heavy rain, waving tree branches, and the water fountain shown in this figure (from top to bottom) pose significant difficulties in detecting accurate foreground regions.

**Quantitative evaluation.** Performance of our proposed methods, RM and AKDE, is evaluated quantitatively on randomly selected samples from different video sequences, taken from [14].

The similarity measure between two regions  $\mathcal{A}$  (detected foreground regions) and  $\mathcal{B}$  (ground truth) is defined by  $\mathcal{S}(\mathcal{A}, \mathcal{B}) = \frac{\mathcal{A} \cap \mathcal{B}}{\mathcal{A} \cup \mathcal{B}}$ . This measure increases monotonically with the similarity between detected masks and the ground truth, ranging between 0 and 1. By using this measure we report the performance of the AKDE method, the RM method, the spatio-temporal technique presented in [14] and the mixture of Gaussians (MoG) in [25]. By comparing the average of the similarity measure over different video sequences in Table 1, we can see that the RM method outperforms



**Fig. 15** Other difficult examples: (a) Original frame. (b) Detected foreground region using AKDE. (c) Detected foreground regions using RM.

other techniques. This shows that the RM method works consistently well on a wide range of video sequences. Also, note that both AKDE and RM are automatic, without the need for fine-tuning a large number of parameters for each scene, as opposed to other existing methods.

However from this table one might argue that AKDE does not perform better than the method presented in [14]. The reason is that in [14] the authors used a morphological post-processing stage to refine their detected foreground regions, while the results shown for AKDE are the raw detected regions. We performed a morphological post-processing on the results obtained by the AKDE, and the average similarity measure increased to 0.74.

**Computation time.** In this section we present a comparison of the speed of the RM and the AKDE on the *Handshake* video sequence. The frame size for the experiments is  $120 \times 160$  in *RGB* color format. The systems are implemented on a 4.8 GHz Pentium 4 Processor. We used  $N = 300$  frames for the initial background training process for the AKDE. Table 2 shows the com-

**Table 2** Computation time.

Method	Detection time per frame (sec)	Speed (fps)
AKDE	0.186	5.2
RM	0.0625	15.38

putation time of the system for the AKDE and the RM method. As seen, the RM method is a fast technique with frame rate of at least 15 fps.

**Comparison summary.** Table 3 summarizes this study and provides a comparison between different tra-

**Table 1** Quantitative evaluation and comparison. The sequences are *Meeting Room*, *Lobby*, *Campus*, *Side Walk*, *Water* and *Fountain*, from left to right from [14].

Method	Videos							Avg. $\mathcal{S}(\mathcal{A}, \mathcal{B})$
	MR	LB	CAM	SW	WAT	FT		
AKDE	0.74	0.66	0.55	0.52	0.84	0.51	0.64	
RM	0.92	0.87	0.75	0.72	0.89	0.87	0.84	
Spatio-Temp[14]	0.91	0.71	0.69	0.57	0.85	0.67	0.74	
MoG[25]	0.44	0.42	0.48	0.36	0.54	0.66	0.49	

**Table 3** Comparison between the proposed methods and traditional techniques.

Criteria	AKDE	RM	KDE [5]	Spatio-Temp[14]	MoG [25]	Wallflower [31]
No. of param.	3	3	3	9	5	8
Scene-independent	Yes	Yes	No	No	No	No
Post proc.	No	No	No	Yes	No	No
Classifier	Bayes	MAP	Bayes	Bayes	Bayes	K-means
Memory req.*	$O(n)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(n)$
Comp. cost*	$O(n)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(n)$

\* : Per-pixel memory requirements or computational cost

$n$ : number of training frames or training features used per pixel

**Table 4** Scenarios where each method appears to be particularly suitable.

Scenario	AKDE	RM	KDE [5]	[14]	MoG [25]	Wallflower [31]
Low contrast video	S*	NS**	S	NS	NS	NS
Close Bg/Fg colors	S	NS	NS	NS	NS	NS
Slowly changing background	NS	S	NS	S	S	S
Rapidly changing background	S	S	S	S	NS	S
Sudden global changes	NS	S	NS	S	S	NS
Non-empty backgrounds	NS	S	NS	S	S	S
Hand-held camera	NS	S	NS	NS	NS	NS

\* : Suitable

\*\* : Not suitable

ditional methods for background modeling proposed in the literature and our proposed methods. The comparison includes the number of parameters, classification type, memory requirements, computation cost and parameter selection. Table 4 shows different scenarios and illustrates which method appears to be particularly suitable for foreground region detection.

## 6 Conclusions and future work

In this paper we have presented two novel techniques for background modeling based on non-parametric density estimation and recursive modeling. The advantage of our adaptive kernel density estimation method (AKDE) over existing techniques is that instead of a global threshold for all pixels in the video scene, different and adaptive thresholds are used for each pixel. By training these thresholds the system works robustly on different video scenes without changing or tuning any parameter. Since each pixel is classified by using adaptive thresholds and exploiting its color dependency, the background model is more accurate.

Our novel recursive modeling method (RM) updates the model on-line when a new frame becomes available, instead of processing a set of video frames to generate the background model. Since the model is not generated by a finite set of samples it eventually converges to the actual background model. This method is superior and more robust than other techniques for situations in which background changes are slow and not periodic.

In particular the RM method outperforms other non-parametric techniques when a set of empty background frames is not available (such as the *Mall* video sequence) as well as in the case of a hand-held camera. The recovery and convergence speed of the RM method in cases when the global illumination suddenly changes are better than those of other non-parametric techniques.

From studying the performance of each of the proposed methods in terms of memory requirements and computational cost it can be observed that the AKDE method is more efficient than the RM technique when background changes are fast. On the other hand when changes occur very slowly, or when there are no empty background frames, the RM works better than AKDE because of its recursive nature.

A future research direction is to perform the foreground/background segmentation without establishing a probabilistic model for the background or the foreground. This new approach would aim to establish the decision boundaries between background and foreground classes for each pixel based on support vector classification methods.

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