In this document, we’ll take a tour of Python’s features suitable for implementing programs in a functional style. After an introduction to the concepts of functional programming, we’ll look at language features such as iterators and generators and relevant library modules such as itertools and functools.

1 Introduction

This section explains the basic concept of functional programming; if you’re just interested in learning about Python language features, skip to the next section.

Programming languages support decomposing problems in several different ways:

- Most programming languages are procedural: programs are lists of instructions that tell the computer what to do with the program’s input. C, Pascal, and even Unix shells are procedural languages.
- In declarative languages, you write a specification that describes the problem to be solved, and the language implementation figures out how to perform the computation efficiently. SQL is the declarative language you’re most likely to be familiar with; a SQL query describes the data set you want to retrieve, and the SQL engine decides whether to scan tables or use indexes, which subclauses should be performed first, etc.
- Object-oriented programs manipulate collections of objects. Objects have internal state and support methods that query or modify this internal state in some way. Smalltalk and Java are object-oriented languages. C++ and Python are languages that support object-oriented programming, but don’t force the use of object-oriented features.
- Functional programming decomposes a problem into a set of functions. Ideally, functions only take inputs and produce outputs, and don’t have any internal state that affects the output produced for a given input. Well-known functional languages include the ML family (Standard ML, OCaml, and other variants) and Haskell.

The designers of some computer languages choose to emphasize one particular approach to programming. This often makes it difficult to write programs that use a different approach. Other languages are multi-paradigm languages that support several different approaches. Lisp, C++, and Python are multi-paradigm; you can write programs or libraries that are largely procedural, object-oriented, or functional in all of these languages. In a large program, different sections might be written using different approaches; the GUI might be object-oriented while the processing logic is procedural or functional, for example.

In a functional program, input flows through a set of functions. Each function operates on its input and produces some output. Functional style discourages functions with side effects that modify internal state or make other changes that aren’t visible in the function’s return value. Functions that have no side effects at all are called purely functional. Avoiding side effects means not using data structures that get updated as a program runs; every function’s output must only depend on its input.

Some languages are very strict about purity and don’t even have assignment statements such as \( a = 3 \) or \( c = a + b \), but it’s difficult to avoid all side effects. Printing to the screen or writing to a disk file are side effects, for example. For example, in Python a `print` statement or a `time.sleep(1)` both return no useful value; they’re only called for their side effects of sending some text to the screen or pausing execution for a second.

Python programs written in functional style usually won’t go to the extreme of avoiding all I/O or all assignments; instead, they’ll provide a functional-appearing interface but will use non-functional features internally. For example,
the implementation of a function will still use assignments to local variables, but won’t modify global variables or have other side effects.

Functional programming can be considered the opposite of object-oriented programming. Objects are little capsules containing some internal state along with a collection of method calls that let you modify this state, and programs consist of making the right set of state changes. Functional programming wants to avoid state changes as much as possible and works with data flowing between functions. In Python you might combine the two approaches by writing functions that take and return instances representing objects in your application (e-mail messages, transactions, etc.).

Functional design may seem like an odd constraint to work under. Why should you avoid objects and side effects? There are theoretical and practical advantages to the functional style:

- Formal provability.
- Modularity.
- Composability.
- Ease of debugging and testing.

### 1.1 Formal provability

A theoretical benefit is that it’s easier to construct a mathematical proof that a functional program is correct.

For a long time researchers have been interested in finding ways to mathematically prove programs correct. This is different from testing a program on numerous inputs and concluding that its output is usually correct, or reading a program’s source code and concluding that the code looks right; the goal is instead a rigorous proof that a program produces the right result for all possible inputs.

The technique used to prove programs correct is to write down invariants, properties of the input data and of the program’s variables that are always true. For each line of code, you then show that if invariants X and Y are true before the line is executed, the slightly different invariants X’ and Y’ are true after the line is executed. This continues until you reach the end of the program, at which point the invariants should match the desired conditions on the program’s output.

Functional programming’s avoidance of assignments arose because assignments are difficult to handle with this technique; assignments can break invariants that were true before the assignment without producing any new invariants that can be propagated onward.

Unfortunately, proving programs correct is largely impractical and not relevant to Python software. Even trivial programs require proofs that are several pages long; the proof of correctness for a moderately complicated program would be enormous, and few or none of the programs you use daily (the Python interpreter, your XML parser, your web browser) could be proven correct. Even if you wrote down or generated a proof, there would then be the question of verifying the proof; maybe there’s an error in it, and you wrongly believe you’ve proved the program correct.

### 1.2 Modularity

A more practical benefit of functional programming is that it forces you to break apart your problem into small pieces. Programs are more modular as a result. It’s easier to specify and write a small function that does one thing than a large function that performs a complicated transformation. Small functions are also easier to read and to check for errors.

### 1.3 Ease of debugging and testing

Testing and debugging a functional-style program is easier.
Debugging is simplified because functions are generally small and clearly specified. When a program doesn’t work, each function is an interface point where you can check that the data are correct. You can look at the intermediate inputs and outputs to quickly isolate the function that’s responsible for a bug.

Testing is easier because each function is a potential subject for a unit test. Functions don’t depend on system state that needs to be replicated before running a test; instead you only have to synthesize the right input and then check that the output matches expectations.

1.4 Composability

As you work on a functional-style program, you’ll write a number of functions with varying inputs and outputs. Some of these functions will be unavoidably specialized to a particular application, but others will be useful in a wide variety of programs. For example, a function that takes a directory path and returns all the XML files in the directory, or a function that takes a filename and returns its contents, can be applied to many different situations.

Over time you’ll form a personal library of utilities. Often you’ll assemble new programs by arranging existing functions in a new configuration and writing a few functions specialized for the current task.

2 Iterators

I’ll start by looking at a Python language feature that’s an important foundation for writing functional-style programs: iterators.

An iterator is an object representing a stream of data; this object returns the data one element at a time. A Python iterator must support a method called next() that takes no arguments and always returns the next element of the stream. If there are no more elements in the stream, next() must raise the StopIteration exception. Iterators don’t have to be finite, though; it’s perfectly reasonable to write an iterator that produces an infinite stream of data.

The built-in iter() function takes an arbitrary object and tries to return an iterator that will return the object’s contents or elements, raising TypeError if the object doesn’t support iteration. Several of Python’s built-in data types support iteration, the most common being lists and dictionaries. An object is called an iterable object if you can get an iterator for it.

You can experiment with the iteration interface manually:

```python
>>> L = [1, 2, 3]
>>> it = iter(L)
>>> print it
<...iterator object at ...>
>>> it.next()
1
>>> it.next()
2
>>> it.next()
3
>>> it.next()
Traceback (most recent call last):
  File "<stdin>", line 1, in ?
StopIteration
```

Python expects iterable objects in several different contexts, the most important being the for statement. In the statement for X in Y, Y must be an iterator or some object for which iter() can create an iterator. These two statements are equivalent:
for i in iter(obj):
    print i

for i in obj:
    print i

Iterators can be materialized as lists or tuples by using the list() or tuple() constructor functions:

```python
>>> L = [1, 2, 3]
>>> iterator = iter(L)
>>> t = tuple(iterator)
>>> t
(1, 2, 3)
```

Sequence unpacking also supports iterators: if you know an iterator will return N elements, you can unpack them into an N-tuple:

```python
>>> L = [1, 2, 3]
>>> iterator = iter(L)
>>> a, b, c = iterator
>>> a, b, c
(1, 2, 3)
```

Built-in functions such as max() and min() can take a single iterator argument and will return the largest or smallest element. The "in" and "not in" operators also support iterators: X in iterator is true if X is found in the stream returned by the iterator. You’ll run into obvious problems if the iterator is infinite; max(), min(), and "not in" will never return, and if the element X never appears in the stream, the "in" operator won’t return either.

Note that you can only go forward in an iterator; there’s no way to get the previous element, reset the iterator, or make a copy of it. Iterator objects can optionally provide these additional capabilities, but the iterator protocol only specifies the next() method. Functions may therefore consume all of the iterator’s output, and if you need to do something different with the same stream, you’ll have to create a new iterator.

### 2.1 Data Types That Support Iterators

We’ve already seen how lists and tuples support iterators. In fact, any Python sequence type, such as strings, will automatically support creation of an iterator.

Calling iter() on a dictionary returns an iterator that will loop over the dictionary’s keys:

```python
>>> m = {'Jan': 1, 'Feb': 2, 'Mar': 3, 'Apr': 4, 'May': 5, 'Jun': 6,
      ... 'Jul': 7, 'Aug': 8, 'Sep': 9, 'Oct': 10, 'Nov': 11, 'Dec': 12}
>>> for key in m:
...     print key, m[key]
Mar 3
Feb 2
Aug 8
Sep 9
Apr 4
Jun 6
Jul 7
Jan 1
May 5
Nov 11
Dec 12
Oct 10
```
Note that the order is essentially random, because it’s based on the hash ordering of the objects in the dictionary.

Applying `iter()` to a dictionary always loops over the keys, but dictionaries have methods that return other iterators. If you want to iterate over keys, values, or key/value pairs, you can explicitly call the `iterkeys()`, `itervalues()`, or `iteritems()` methods to get an appropriate iterator.

The `dict()` constructor can accept an iterator that returns a finite stream of `(key, value)` tuples:

```python
>>> L = [('Italy', 'Rome'), ('France', 'Paris'), ('US', 'Washington DC')]
>>> dict(iter(L))
{'Italy': 'Rome', 'US': 'Washington DC', 'France': 'Paris'}
```

Files also support iteration by calling the `readline()` method until there are no more lines in the file. This means you can read each line of a file like this:

```python
for line in file:
    # do something for each line
```

Sets can take their contents from an iterable and let you iterate over the set’s elements:

```python
S = set((2, 3, 5, 7, 11, 13))
for i in S:
    print i
```

### 3 Generator expressions and list comprehensions

Two common operations on an iterator’s output are 1) performing some operation for every element, 2) selecting a subset of elements that meet some condition. For example, given a list of strings, you might want to strip off trailing whitespace from each line or extract all the strings containing a given substring.

List comprehensions and generator expressions (short form: “listcomps” and “genexps”) are a concise notation for such operations, borrowed from the functional programming language Haskell ([http://www.haskell.org](http://www.haskell.org)). You can strip all the whitespace from a stream of strings with the following code:

```python
line_list = [' line 1
', 'line 2  
', ' ... ]
# Generator expression -- returns iterator
stripped_iter = (line.strip() for line in line_list)
# List comprehension -- returns list
stripped_list = [line.strip() for line in line_list]
```

You can select only certain elements by adding an "if" condition:

```python
stripped_list = [line.strip() for line in line_list
                   if line != ' ']
```

With a list comprehension, you get back a Python list; `stripped_list` is a list containing the resulting lines, not an iterator. Generator expressions return an iterator that computes the values as necessary, not needing to materialize all the values at once. This means that list comprehensions aren’t useful if you’re working with iterators that return an infinite stream or a very large amount of data. Generator expressions are preferable in these situations.

Generator expressions are surrounded by parentheses (“()”) and list comprehensions are surrounded by square brackets (“[]”). Generator expressions have the form:

```python
( expression for expr in sequence1
    if condition1
    for expr2 in sequence2
```
if condition2
        for expr3 in sequence3 ...
    if condition3
        for exprN in sequenceN
    if conditionN )

Again, for a list comprehension only the outside brackets are different (square brackets instead of parentheses).

The elements of the generated output will be the successive values of expression. The if clauses are all optional; if present, expression is only evaluated and added to the result when condition is true.

Generator expressions always have to be written inside parentheses, but the parentheses signalling a function call also count. If you want to create an iterator that will be immediately passed to a function you can write:

    obj_total = sum(obj.count for obj in list_all_objects())

The for...in clauses contain the sequences to be iterated over. The sequences do not have to be the same length, because they are iterated over from left to right, not in parallel. For each element in sequence1, sequence2 is looped over from the beginning. sequence3 is then looped over for each resulting pair of elements from sequence1 and sequence2.

To put it another way, a list comprehension or generator expression is equivalent to the following Python code:

```python
for expr1 in sequence1:
    if not (condition1):
        continue  # Skip this element
    for expr2 in sequence2:
        if not (condition2):
            continue  # Skip this element
    ...
    for exprN in sequenceN:
        if not (conditionN):
            continue  # Skip this element

    # Output the value of
    # the expression.
```

This means that when there are multiple for...in clauses but no if clauses, the length of the resulting output will be equal to the product of the lengths of all the sequences. If you have two lists of length 3, the output list is 9 elements long:

```python
>>> seq1 = 'abc'
>>> seq2 = (1,2,3)
>>> [(x,y) for x in seq1 for y in seq2]
[('a', 1), ('a', 2), ('a', 3),
 ('b', 1), ('b', 2), ('b', 3),
 ('c', 1), ('c', 2), ('c', 3)]
```

To avoid introducing an ambiguity into Python’s grammar, if expression is creating a tuple, it must be surrounded with parentheses. The first list comprehension below is a syntax error, while the second one is correct:

```python
# Syntax error
[ x,y for x in seq1 for y in seq2]
# Correct
[ (x,y) for x in seq1 for y in seq2]```
Generators

Generators are a special class of functions that simplify the task of writing iterators. Regular functions compute a value and return it, but generators return an iterator that returns a stream of values.

You’re doubtless familiar with how regular function calls work in Python or C. When you call a function, it gets a private namespace where its local variables are created. When the function reaches a return statement, the local variables are destroyed and the value is returned to the caller. A later call to the same function creates a new private namespace and a fresh set of local variables. But, what if the local variables weren’t thrown away on exiting a function? What if you could later resume the function where it left off? This is what generators provide; they can be thought of as resumable functions.

Here’s the simplest example of a generator function:

```python
def generate_ints(N):
    for i in range(N):
        yield i
```

Any function containing a yield keyword is a generator function; this is detected by Python’s bytecode compiler which compiles the function specially as a result.

When you call a generator function, it doesn’t return a single value; instead it returns a generator object that supports the iterator protocol. On executing the yield expression, the generator outputs the value of i, similar to a return statement. The big difference between yield and a return statement is that on reaching a yield the generator’s state of execution is suspended and local variables are preserved. On the next call to the generator’s .next() method, the function will resume executing.

Here’s a sample usage of the generate_ints() generator:

```python
>>> gen = generate_ints(3)
>>> gen
<generator object generate_ints at ...>
>>> gen.next()
0
>>> gen.next()
1
>>> gen.next()
2
>>> gen.next()
Traceback (most recent call last):
  File "stdin", line 1, in ?
  File "stdin", line 2, in generate_ints
StopIteration
```

You could equally write for i in generate_ints(5), or a, b, c = generate_ints(3).

Inside a generator function, the return statement can only be used without a value, and signals the end of the procession of values; after executing a return the generator cannot return any further values. return with a value, such as return 5, is a syntax error inside a generator function. The end of the generator’s results can also be indicated by raising StopIteration manually, or by just letting the flow of execution fall off the bottom of the function.

You could achieve the effect of generators manually by writing your own class and storing all the local variables of the generator as instance variables. For example, returning a list of integers could be done by setting self.count to 0, and having the next() method increment self.count and return it. However, for a moderately complicated generator, writing a corresponding class can be much messier.

The test suite included with Python’s library, test_generators.py, contains a number of more interesting examples. Here’s one generator that implements an in-order traversal of a tree using generators recursively.
# A recursive generator that generates Tree leaves in in-order.

def inorder(t):
    if t:
        for x in inorder(t.left):
            yield x
        yield t.label
        for x in inorder(t.right):
            yield x

Two other examples in test_generators.py produce solutions for the N-Queens problem (placing N queens on an N\times N chess board so that no queen threatens another) and the Knight’s Tour (finding a route that takes a knight to every square of an N\times N chessboard without visiting any square twice).

4.1 Passing values into a generator

In Python 2.4 and earlier, generators only produced output. Once a generator’s code was invoked to create an iterator, there was no way to pass any new information into the function when its execution is resumed. You could hack together this ability by making the generator look at a global variable or by passing in some mutable object that callers then modify, but these approaches are messy.

In Python 2.5 there’s a simple way to pass values into a generator. \texttt{yield} became an expression, returning a value that can be assigned to a variable or otherwise operated on:

\[
\text{val} = \text{(yield i)}
\]

I recommend that you \textbf{always} put parentheses around a \texttt{yield} expression when you’re doing something with the returned value, as in the above example. The parentheses aren’t always necessary, but it’s easier to always add them instead of having to remember when they’re needed.

(PEP 342 explains the exact rules, which are that a \texttt{yield}-expression must always be parenthesized except when it occurs at the top-level expression on the right-hand side of an assignment. This means you can write \texttt{val = yield i} but have to use parentheses when there’s an operation, as in \texttt{val = (yield i) + 12}.)

Values are sent into a generator by calling its \texttt{send(value)} method. This method resumes the generator’s code and the \texttt{yield} expression returns the specified value. If the regular \texttt{next()} method is called, the \texttt{yield} returns \texttt{None}.

Here’s a simple counter that increments by 1 and allows changing the value of the internal counter.

def counter (maximum):
    i = 0
    while i < maximum:
        val = \text{(yield i)}
        # If value provided, change counter
        if val is not None:
            i = val
        else:
            i += 1

And here’s an example of changing the counter:

>>> it = counter(10)
>>> print it.next()
0
>>> print it.next()
1
>>> print it.send(8)
Because *yield* will often be returning *None*, you should always check for this case. Don’t just use its value in expressions unless you’re sure that the *send()* method will be the only method used resume your generator function.

### 5 Built-in functions

Let’s look in more detail at built-in functions often used with iterators.

Two of Python’s built-in functions, *map()* and *filter()* are somewhat obsolete; they duplicate the features of list comprehensions but return actual lists instead of iterators.

```python
>>> def upper(s):
...     return s.upper()

>>> map(upper, [’sentence’, ’fragment’])
[’SENTENCE’, ’FRAGMENT’]

>>> [upper(s) for s in [’sentence’, ’fragment’]]
[’SENTENCE’, ’FRAGMENT’]
```

As shown above, you can achieve the same effect with a list comprehension. The *itertools.imap()* function does the same thing but can handle infinite iterators; it’ll be discussed later, in the section on the *itertools* module.

`*filter()*` returns a list that contains all the sequence elements that meet a certain condition, and is similarly duplicated by list comprehensions. A *predicate* is a function that returns the truth value of some condition; for use with *filter()* the predicate must take a single value.

```python
>>> def is_even(x):
...     return (x % 2) == 0
```
filter(is_even, range(10))
[0, 2, 4, 6, 8]

This can also be written as a list comprehension:

[x for x in range(10) if is_even(x)]
[0, 2, 4, 6, 8]

filter() also has a counterpart in the itertools module, itertools.ifilter(), that returns an iterator and can therefore handle infinite sequences just as itertools.imap() can.

reduce(func, iter, [initial_value]) doesn't have a counterpart in the itertools module because it cumulatively performs an operation on all the iterable’s elements and therefore can’t be applied to infinite iterables. func must be a function that takes two elements and returns a single value. reduce() takes the first two elements A and B returned by the iterator and calculates func(A, B). It then requests the third element, C, calculates func(func(A, B), C), combines this result with the fourth element returned, and continues until the iterable is exhausted. If the iterable returns no values at all, a TypeError exception is raised. If the initial value is supplied, it’s used as a starting point and func(initial_value, A) is the first calculation.

>>> import operator
>>> reduce(operator.concat, ['A', 'BB', 'C'])
'ABBC'
>>> reduce(operator.concat, [])
Traceback (most recent call last):
  ...
TypeError: reduce() of empty sequence with no initial value

>>> reduce(operator.mul, [1, 2, 3], 1)
6
>>> reduce(operator.mul, [], 1)
1

If you use operator.add() with reduce(), you’ll add up all the elements of the iterable. This case is so common that there’s a special built-in called sum() to compute it:

>>> reduce(operator.add, [1, 2, 3, 4], 0)
10
>>> sum([1, 2, 3, 4])
10
>>> sum([])
0

For many uses of reduce(), though, it can be clearer to just write the obvious for loop:

# Instead of:
product = reduce(operator.mul, [1, 2, 3], 1)

# You can write:
product = 1
for i in [1, 2, 3]:
    product *= i

enumerate(iter) counts off the elements in the iterable, returning 2-tuples containing the count and each element.

>>> for item in enumerate(['subject', 'verb', 'object']):
    ...     print item
(0, 'subject')
(1, 'verb')
(2, 'object')
enumerate() is often used when looping through a list and recording the indexes at which certain conditions are met:

```python
def open(file, mode):
    for i, line in enumerate(f):
        if line.strip() == '':
            print(f'Blank line at line #\d{i}\''
sorted(iterable, [cmp=None], [key=None], [reverse=False]) collects all the elements of the iterable into a list, sorts the list, and returns the sorted result. The cmp, key, and reverse arguments are passed through to the constructed list’s .sort() method.

```python
>>> import random
>>> # Generate 8 random numbers between [0, 10000)
>>> rand_list = random.sample(range(10000), 8)
>>> rand_list
[769, 7953, 9828, 8442, 9878, 6213, 2207]
>>> sorted(rand_list)
[769, 2207, 6213, 6431, 7953, 7953, 9878, 9878]
>>> sorted(rand_list, reverse=True)
[9878, 9828, 8442, 7953, 6431, 6213, 2207, 769]
```

(For a more detailed discussion of sorting, see the Sorting mini-HOWTO in the Python wiki at http://wiki.python.org/moin/HowTo/Sorting.)

6 Small functions and the lambda expression

When writing functional-style programs, you’ll often need little functions that act as predicates or that combine elements in some way.

If there’s a Python built-in or a module function that’s suitable, you don’t need to define a new function at all:

```python
stripped_lines = [line.strip() for line in lines]
existing_files = filter(os.path.exists, file_list)
```

If the function you need doesn’t exist, you need to write it. One way to write small functions is to use the lambda statement. lambda takes a number of parameters and an expression combining these parameters, and creates a small function that returns the value of the expression:

```python
lowercase = lambda x: x.lower()```
print_assign = \texttt{lambda} \ text{name}, \text{value}: \text{name} + '=' + \text{str(value)}

adder = \texttt{lambda} \ x, \ y: x+y

An alternative is to just use the \texttt{def} statement and define a function in the usual way:

\begin{verbatim}
def lowercase(x):
    return x.lower()

def print_assign(name, value):
    return name + '=' + str(value)

def adder(x,y):
    return x+y
\end{verbatim}

Which alternative is preferable? That’s a style question; my usual course is to avoid using \texttt{lambda}.

One reason for my preference is that \texttt{lambda} is quite limited in the functions it can define. The result has to be computable as a single expression, which means you can’t have multiway \texttt{if}... \texttt{elif}... \texttt{else} comparisons or \texttt{try}... \texttt{except} statements. If you try to do too much in a \texttt{lambda} statement, you’ll end up with an overly complicated expression that’s hard to read. Quick, what’s the following code doing?

\begin{verbatim}
total = \texttt{reduce}(\texttt{lambda} \ a, \ b: (0, a[1] + b[1]), \text{items})[1]
\end{verbatim}

You can figure it out, but it takes time to disentangle the expression to figure out what’s going on. Using a short nested \texttt{def} statements makes things a little bit better:

\begin{verbatim}
def combine (a, b):
    return 0, a[1] + b[1]

def adder(x,y):
    return x+y

def print_assign(name, value):
    return name + '=' + str(value)

def lowercase(x):
    return x.lower()
\end{verbatim}

\begin{verbatim}
total = \texttt{reduce}(combine, \text{items})[1]
\end{verbatim}

But it would be best of all if I had simply used a \texttt{for} loop:

\begin{verbatim}
total = 0
for a, b in \text{items}:
    total += b
\end{verbatim}

Or the \texttt{sum()} built-in and a generator expression:

\begin{verbatim}
total = \texttt{sum}(b \text{ for } a,b \text{ in } \text{items})
\end{verbatim}

Many uses of \texttt{reduce()} are clearer when written as \texttt{for} loops.

Fredrik Lundh once suggested the following set of rules for refactoring uses of \texttt{lambda}:

1. Write a \texttt{lambda} function.
2. Write a comment explaining what the heck that \texttt{lambda} does.
3. Study the comment for a while, and think of a name that captures the essence of the comment.
4. Convert the \texttt{lambda} to a \texttt{def} statement, using that name.
5. Remove the comment.

I really like these rules, but you’re free to disagree about whether this lambda-free style is better.

\section{The \texttt{itertools} module}

The \texttt{itertools} module contains a number of commonly-used iterators as well as functions for combining several iterators. This section will introduce the module’s contents by showing small examples.
The module’s functions fall into a few broad classes:

- Functions that create a new iterator based on an existing iterator.
- Functions for treating an iterator’s elements as function arguments.
- Functions for selecting portions of an iterator’s output.
- A function for grouping an iterator’s output.

### 7.1 Creating new iterators

`itertools.count(n)` returns an infinite stream of integers, increasing by 1 each time. You can optionally supply the starting number, which defaults to 0:

- `itertools.count()` => …
- `itertools.count(10)` => 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, …

`itertools.cycle(iter)` saves a copy of the contents of a provided iterable and returns a new iterator that returns its elements from first to last. The new iterator will repeat these elements infinitely.

- `itertools.cycle([1, 2, 3, 4, 5])` => 1, 2, 3, 4, 5, 1, 2, 3, 4, 5, …

`itertools.repeat(elem, [n])` returns the provided element `n` times, or returns the element endlessly if `n` is not provided.

- `itertools.repeat('abc')` => abc, abc, abc, abc, abc, abc, abc, abc, abc, ...
- `itertools.repeat('abc', 5)` => abc, abc, abc, abc, abc

`itertools.chain(iterA, iterB, ...)` takes an arbitrary number of iterables as input, and returns all the elements of the first iterator, then all the elements of the second, and so on, until all of the iterables have been exhausted.

- `itertools.chain(['a', 'b', 'c'], [1, 2, 3])` => a, b, c, 1, 2, 3

`itertools.izip(iterA, iterB, ...)` takes one element from each iterable and returns them in a tuple:

- `itertools.izip(['a', 'b', 'c'], (1, 2, 3))` => ("a", 1), ("b", 2), ("c", 3)

It’s similar to the built-in `zip()` function, but doesn’t construct an in-memory list and exhaust all the input iterators before returning; instead tuples are constructed and returned only if they’re requested. (The technical term for this behaviour is lazy evaluation.)

This iterator is intended to be used with iterables that are all of the same length. If the iterables are of different lengths, the resulting stream will be the same length as the shortest iterable.

- `itertools.islice(iter, [start], stop, [step])` returns a stream that’s a slice of the iterator. With a single `stop` argument, it will return the first `stop` elements. If you supply a starting index, you’ll get `stop-start`
elements, and if you supply a value for `step`, elements will be skipped accordingly. Unlike Python’s string and list slicing, you can’t use negative values for `start`, `stop`, or `step`.

```python
itertools.islice(range(10), 8) => 0, 1, 2, 3, 4, 5, 6, 7
itertools.islice(range(10), 2, 8) => 2, 3, 4, 5, 6, 7
itertools.islice(range(10), 2, 8, 2) => 2, 4, 6
```

`itertools.tee` replicates an iterator; it returns `n` independent iterators that will all return the contents of the source iterator. If you don’t supply a value for `n`, the default is 2. Replicating iterators requires saving some of the contents of the source iterator, so this can consume significant memory if the iterator is large and one of the new iterators is consumed more than the others.

```python
itertools.tee(itertools.count()) => iterA, iterB
where iterA -> 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ...
and iterB -> 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ...
```

### 7.2 Calling functions on elements

Two functions are used for calling other functions on the contents of an iterable.

```python
itertools.imap(f, iterA, iterB, ...) returns a stream containing f(iterA[0], iterB[0]), f(iterA[1], iterB[1]), f(iterA[2], iterB[2]), ...

itertools.imap(operator.add, [5, 6, 5], [1, 2, 3]) => 6, 8, 8
```

The `operator` module contains a set of functions corresponding to Python’s operators. Some examples are `operator.add(a, b)` (adds two values), `operator.ne(a, b)` (same as `a!=b`), and `operator.attrgetter('id')` (returns a callable that fetches the "id" attribute).

```python
itertools.starmap(func, iter) assumes that the iterable will return a stream of tuples, and calls `f()` using these tuples as the arguments:

itertools.starmap(os.path.join, [('/usr', 'bin', 'java'), ('/bin', 'python'), ('/usr', 'bin', 'perl'), ('/usr', 'bin', 'ruby')]) => /usr/bin/java, /bin/python, /usr/bin/perl, /usr/bin/ruby
```

### 7.3 Selecting elements

Another group of functions chooses a subset of an iterator’s elements based on a predicate.

```python
itertools.ifilter(predicate, iter) returns all the elements for which the predicate returns true:

```python
def is_even(x):
    return (x % 2) == 0


```python
itertools.ifilter(is_even, itertools.count()) => 0, 2, 4, 6, 8, 10, 12, 14, ...

itertools.ifilterfalse(predicate, iter) is the opposite, returning all elements for which the predicate returns false:

itertools.ifilterfalse(is_even, itertools.count()) => 1, 3, 5, 7, 9, 11, 13, 15, ...

itertools.takewhile(predicate, iter) returns elements for as long as the predicate returns true. Once the predicate returns false, the iterator will signal the end of its results.

def less_than_10(x):
    return (x < 10)

itertools.takewhile(less_than_10, itertools.count()) => 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

itertools.takewhile(is_even, itertools.count()) => 0

itertools.dropwhile(predicate, iter) discards elements while the predicate returns true, and then returns the rest of the iterable’s results.

itertools.dropwhile(less_than_10, itertools.count()) => 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, ...

itertools.dropwhile(is_even, itertools.count()) => 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, ...

7.4 Grouping elements

The last function I’ll discuss, itertools.groupby(iter, key_func=None), is the most complicated. key_func(elem) is a function that can compute a key value for each element returned by the iterable. If you don’t supply a key function, the key is simply each element itself.

groupby() collects all the consecutive elements from the underlying iterable that have the same key value, and returns a stream of 2-tuples containing a key value and an iterator for the elements with that key.

city_list = [('Decatur', 'AL'), ('Huntsville', 'AL'), ('Selma', 'AL'),
            ('Anchorage', 'AK'), ('Nome', 'AK'),
            ('Flagstaff', 'AZ'), ('Phoenix', 'AZ'), ('Tucson', 'AZ'),
            ...]

def get_state ((city, state)):
    return state

itertools.groupby(city_list, get_state) =>
    ('AL', iterator-1),
    ('AK', iterator-2),
    ('AZ', iterator-3), ...

where
iterator-1 =>
    ('Decatur', 'AL'), ('Huntsville', 'AL'), ('Selma', 'AL')
iterator-2 =>
```

('Anchorage', 'AK'), ('Nome', 'AK')
iterator-3 =>
('Flagstaff', 'AZ'), ('Phoenix', 'AZ'), ('Tucson', 'AZ')
groupby() assumes that the underlying iterable’s contents will already be sorted based on the key. Note that the returned iterators also use the underlying iterable, so you have to consume the results of iterator-1 before requesting iterator-2 and its corresponding key.

8 The functools module

The functools module in Python 2.5 contains some higher-order functions. A higher-order function takes one or more functions as input and returns a new function. The most useful tool in this module is the functools.partial() function.

For programs written in a functional style, you’ll sometimes want to construct variants of existing functions that have some of the parameters filled in. Consider a Python function f(a, b, c); you may wish to create a new function g(b, c) that’s equivalent to f(1, b, c); you’re filling in a value for one of f()’s parameters. This is called “partial function application”.

The constructor for partial takes the arguments (function, arg1, arg2, ... kwarg1=value1, kwarg2=value2). The resulting object is callable, so you can just call it to invoke function with the filled-in arguments.

Here’s a small but realistic example:

```python
import functools

def log (message, subsystem):
    "Write the contents of 'message' to the specified subsystem."
    print '%s: %s' % (subsystem, message)
    ...

server_log = functools.partial(log, subsystem='server')
server_log('Unable to open socket')
```

8.1 The operator module

The operator module was mentioned earlier. It contains a set of functions corresponding to Python’s operators. These functions are often useful in functional-style code because they save you from writing trivial functions that perform a single operation.

Some of the functions in this module are:

- Math operations: add(), sub(), mul(), div(), floordiv(), abs(), ...
- Logical operations: not_(), truth().
- Bitwise operations: and_(), or_(), invert().
- Comparisons: eq(), ne(), lt(), le(), gt(), and ge().
- Object identity: is_(), is_not().

Consult the operator module’s documentation for a complete list.
8.2 The functional module

Collin Winter’s functional module provides a number of more advanced tools for functional programming. It also reimplements several Python built-ins, trying to make them more intuitive to those used to functional programming in other languages.

This section contains an introduction to some of the most important functions in functional; full documentation can be found at the project’s website.

compose(outer, inner, unpack=False)

The compose() function implements function composition. In other words, it returns a wrapper around the outer and inner callables, such that the return value from inner is fed directly to outer. That is,

```python
>>> def add(a, b):
...     return a + b
...
>>> def double(a):
...     return 2 * a
...
>>> compose(double, add)(5, 6)
22
```

is equivalent to

```python
>>> double(add(5, 6))
22
```

The unpack keyword is provided to work around the fact that Python functions are not always fully curried. By default, it is expected that the inner function will return a single object and that the outer function will take a single argument. Setting the unpack argument causes compose to expect a tuple from inner which will be expanded before being passed to outer. Put simply,

compose(f, g)(5, 6)

is equivalent to:

```python
f(g(5, 6))
```

while

compose(f, g, unpack=True)(5, 6)

is equivalent to:

```python
f(*g(5, 6))
```

Even though compose() only accepts two functions, it’s trivial to build up a version that will compose any number of functions. We’ll use reduce(), compose() and partial() (the last of which is provided by both functional and functools).

```python
from functional import compose, partial

multi_compose = partial(reduce, compose)
```

We can also use map(), compose() and partial() to craft a version of "\".join(...) that converts its arguments to string:

```python
from functional import compose, partial

join = compose("\".join, partial(map, str))
```
flip(func)

flip() wraps the callable in func and causes it to receive its non-keyword arguments in reverse order.

>>> def triple(a, b, c):
...    return (a, b, c)
...
>>> triple(5, 6, 7)
(5, 6, 7)
>>> flipped_triple = flip(triple)
>>> flipped_triple(5, 6, 7)
(7, 6, 5)

foldl(func, start, iterable)

foldl() takes a binary function, a starting value (usually some kind of ‘zero’), and an iterable. The function is applied to the starting value and the first element of the list, then the result of that and the second element of the list, then the result of that and the third element of the list, and so on.

This means that a call such as:

foldl(f, 0, [1, 2, 3])

is equivalent to:

f(f(f(0, 1), 2), 3)

foldl() is roughly equivalent to the following recursive function:

```python
def foldl(func, start, seq):
    if len(seq) == 0:
        return start
    return foldl(func, func(start, seq[0]), seq[1:1])
```

Speaking of equivalence, the above foldl call can be expressed in terms of the built-in reduce like so:

reduce(f, [1, 2, 3], 0)

We can use foldl(), operator.concat() and partial() to write a cleaner, more aesthetically-pleasing version of Python’s "".join(...) idiom:

```python
from functional import foldl, partial from operator import concat

join = partial(foldl, concat, "")
```

9 Revision History and Acknowledgements

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Version 0.1: posted June 30 2006.
Version 0.11: posted July 1 2006. Typo fixes.
Version 0.2: posted July 10 2006. Merged genexp and listcomp sections into one. Typo fixes.
Version 0.21: Added more references suggested on the tutor mailing list.
Version 0.30: Adds a section on the `functional` module written by Collin Winter; adds short section on the `operator` module; a few other edits.

10 References

10.1 General

*Structure and Interpretation of Computer Programs*, by Harold Abelson and Gerald Jay Sussman with Julie Sussman. Full text at [http://mitpress.mit.edu/sicp/](http://mitpress.mit.edu/sicp/). In this classic textbook of computer science, chapters 2 and 3 discuss the use of sequences and streams to organize the data flow inside a program. The book uses Scheme for its examples, but many of the design approaches described in these chapters are applicable to functional-style Python code.

[http://www.defmacro.org/ramblings/fp.html](http://www.defmacro.org/ramblings/fp.html): A general introduction to functional programming that uses Java examples and has a lengthy historical introduction.


10.2 Python-specific


Mertz also wrote a 3-part series of articles on functional programming for IBM’s DeveloperWorks site; see [part 1](http://www.ibm.com/developerworks/), [part 2](http://www.ibm.com/developerworks/), and [part 3](http://www.ibm.com/developerworks/),

10.3 Python documentation

Documentation for the `itertools` module.

Documentation for the `operator` module.

**PEP 289**: “Generator Expressions”

**PEP 342**: “Coroutines via Enhanced Generators” describes the new generator features in Python 2.5.
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